#### Lecture 31

CSE 331 Nov 14, 2016

# Mini project video due TODAY

#### note 🕆

#### Mini project video

Sorry for the delay in posting this information. For the basics, please see the mini-project page.

Below are the main logistics. IT IS IMPORTANT TO READ THESE CAREFULLY SINCE NOT FOLLOWING INSTRUCTION COULD LEAD TO LOSS OF ALL POINTS.

- The deadline is Monday, November 14, 11:59pm. You can start submitting on Autolab anytime from now till the deadline.
- You will need to need to form your group on Autolab again for this submission. See @304 for instructions on how to do it.
  - Very important: Please make sure you submit your group's submission after the group has been formed. If this is not done, the entire group will get a zero.
    - No excuses on this-- make sure you do this group formation well in advance. If you cannot reach one of your group
      members at the last moment, then that is your problem.
- You will need to submit a PDF with the following information:
  - · Link to the your group's video on Youtube
    - The video has to be for AT MOST FIVE (5) MINS. While gra ignored. Of course a shorter video is fine!
  - If you would prefer your groups video to be not listed on this page all videos will be linked to on the above page.
  - If you submit in a format other than PDF then your group will get a zero. Also make the review the submitted PDF to double-check that Autolab can actually read your submitted file.

Make sure you follow ALL instructions else you will lose points

stop following

126 views

Actions

default

#### **Comments on feedback**

#### note 🖄

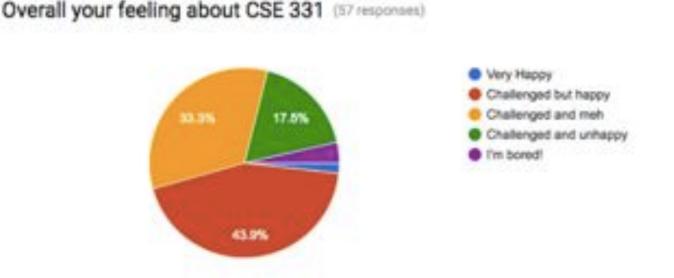
O views

#### Comments on feedback

Thanks for everyone who have feedback (@627). Over the course of this week, I will address/respond to some of the feedback (both the quantitative ones and the written comments).

In some cases I will be able to incorporate your comments this year. For others, it might not be but I will at least present you my rationale for for why not.

To being with here is the overall response:



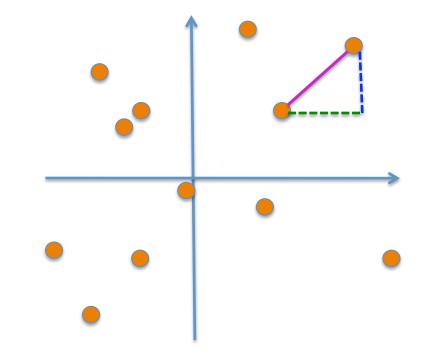
Of course in an ideal world. I would like all the reconnect to be either blue or red. Of most concern in the 17.5% in orean and this

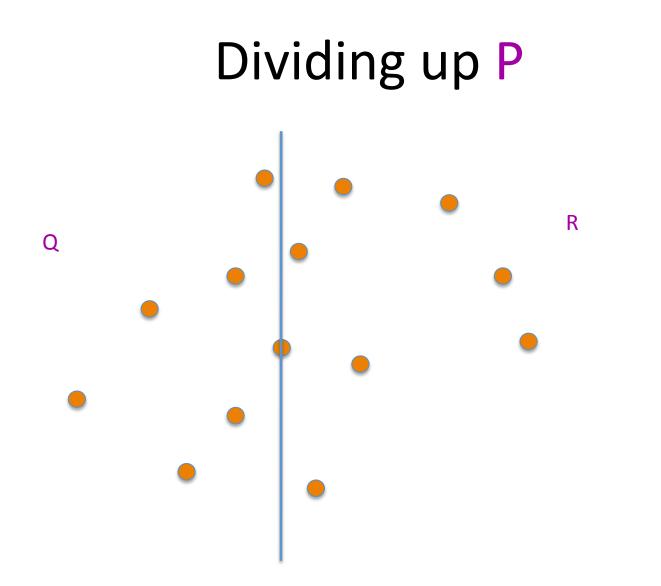
#### **Closest pairs of points**

Input: n 2-D points  $P = \{p_1, ..., p_n\}; p_i = (x_i, y_i)$ 

 $d(p_i, p_i) = ((x_i - x_i)^2 + (y_i - y_i)^2)^{1/2}$ 

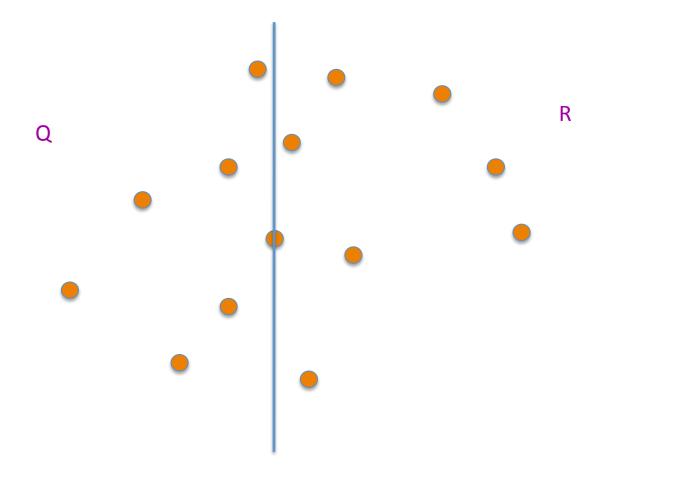
Output: Points p and q that are closest





First n/2 points according to the x-coord

#### Recursively find closest pairs

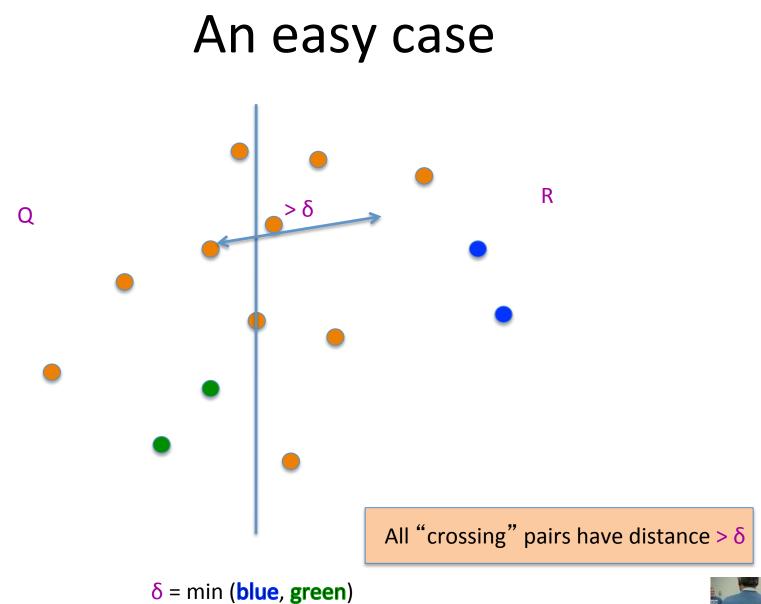


 $\delta$  = min (**blue**, green)

#### An aside: maintain sorted lists

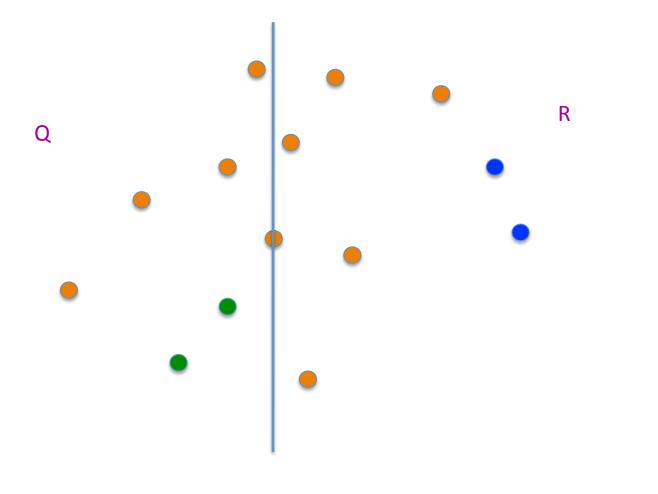
 $P_x$  and  $P_y$  are P sorted by x-coord and y-coord

 $Q_x$ ,  $Q_y$ ,  $R_x$ ,  $R_y$  can be computed from  $P_x$  and  $P_y$  in O(n) time





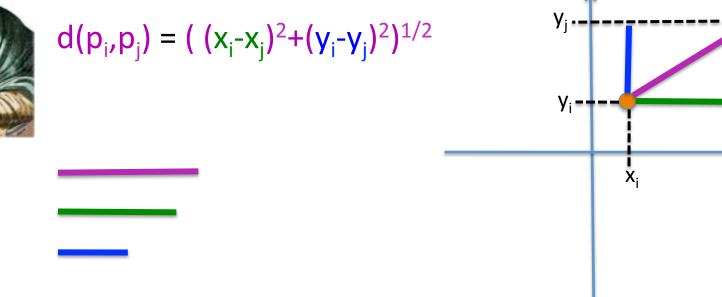
#### Life is not so easy though



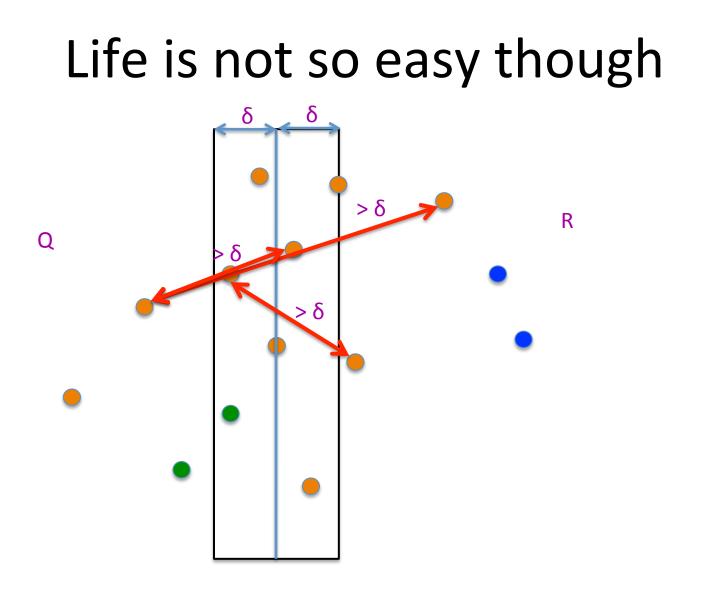
δ = min (**blue**, green)

# Euclid to the rescue (?)



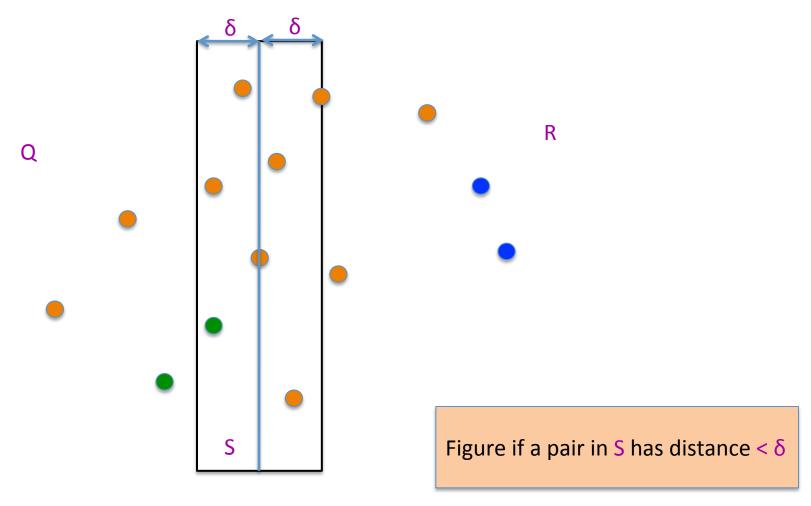


The distance is larger than the **x** or **y**-coord difference



 $\delta$  = min (**blue**, green)

#### All we have to do now



 $\delta$  = min (**blue**, green)

# The algorithm so far...

Input: n 2-D points  $P = \{p_1, ..., p_n\}; p_i = (x_i, y_i)$ 

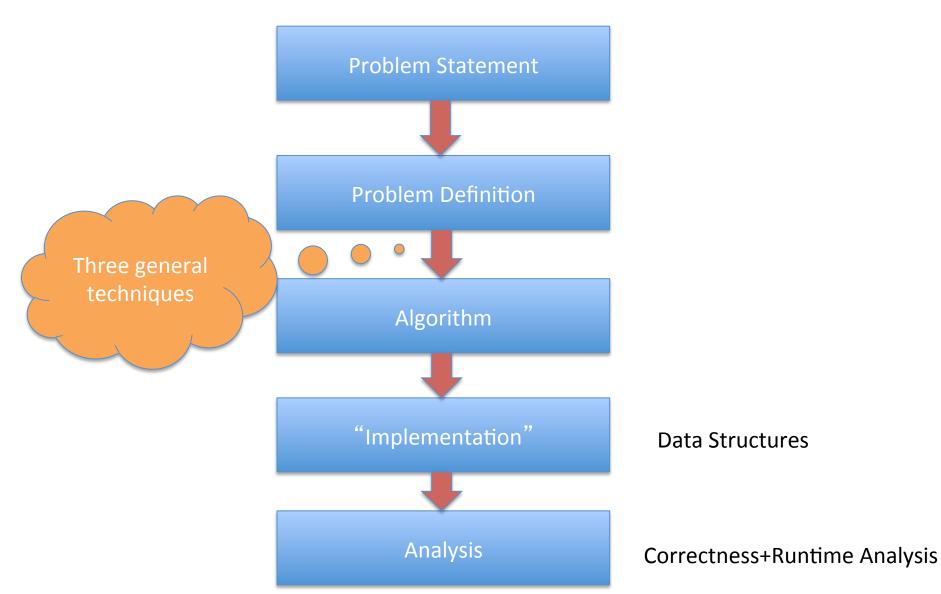
 $O(n \log n) + T(n)$ 

Sort P to get  $P_x$  and  $P_{y}$ O(n log n) T(< 4) = cClosest-Pair (P<sub>x</sub>, P<sub>y</sub>) T(n) = 2T(n/2) + cnIf n < 4 then find closest point by brute-force **Q** is first half of  $P_x$  and **R** is the rest O(n) Compute  $Q_x$ ,  $Q_y$ ,  $R_x$  and  $R_y$ O(n) O(n log n) overall  $(q_0, q_1) = Closest-Pair (Q_x, Q_y)$  $(r_0, r_1) = Closest-Pair (R_x, R_y)$ O(n) $\delta = \min(d(q_0, q_1), d(r_0, r_1))$ O(n) S = points (x,y) in P s.t.  $|x - x^*| < \delta$ return Closest-in-box (S,  $(q_0, q_1)$ ,  $(r_0, r_1)$ ) Assume can be done in O(n)

#### Rest of today's agenda

Implement Closest-in-box in O(n) time

### High level view of CSE 331



### **Greedy Algorithms**

#### Natural algorithms



Reduced exponential running time to polynomial

### **Divide and Conquer**

Recursive algorithmic paradigm



Reduced large polynomial time to smaller polynomial time

#### A new algorithmic technique

**Dynamic Programming** 

# Dynamic programming vs. Divide & Conquer



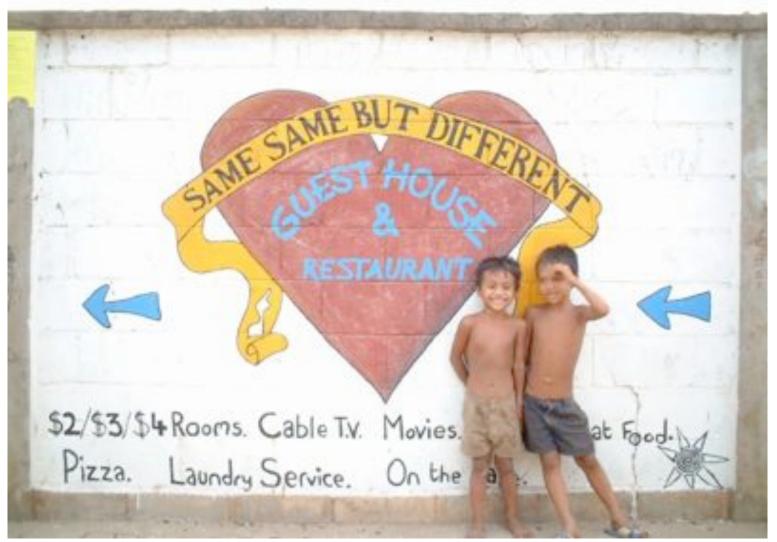
#### Same same because

Both design recursive algorithms



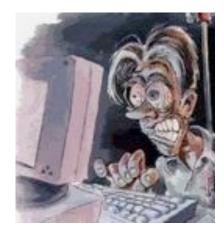
#### Different because

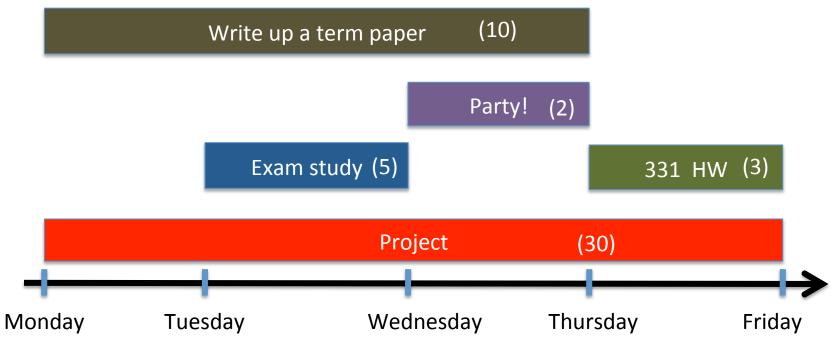
Dynamic programming is smarter about solving recursive sub-problems



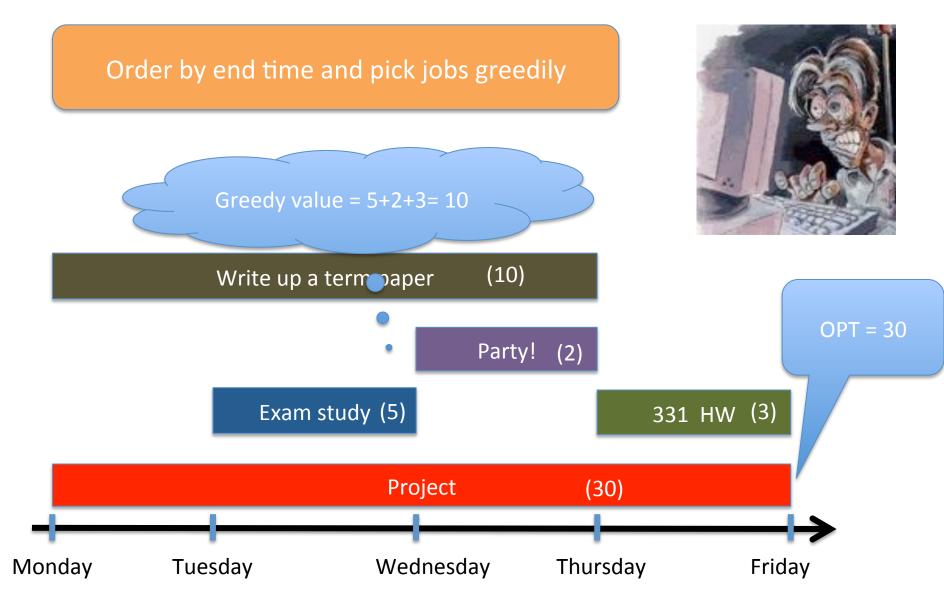
### End of Semester blues

Can only do one thing at any day: what is the optimal schedule to obtain maximum value?





#### Previous Greedy algorithm



### Today's agenda

Formal definition of the problem

Start designing a recursive algorithm for the problem

