

Lecture 32

CSE 331

Nov 16, 2016

Talk today

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Buffalo Talks | How to crack the coding interviews?

Buffalo Talks has their next talk ready! Sai Vikneshwar, a theoretical computer science major at UB is going to talk about "How to crack the coding interviews?".

He has interviewed with tonnes of companies and failed many times, but there were times when he didn't fail and got offers from companies like Google, Microsoft, Fb, etc. Sai is going to share all his experiences and how he did it.

I assure you, Sai's talk will serve as a great motivation for many of you who are currently in the interviewing process, so don't miss out on this one.

Date and Time - 11/16 (Wed) at 6:00 pm
Venue - Knox 109

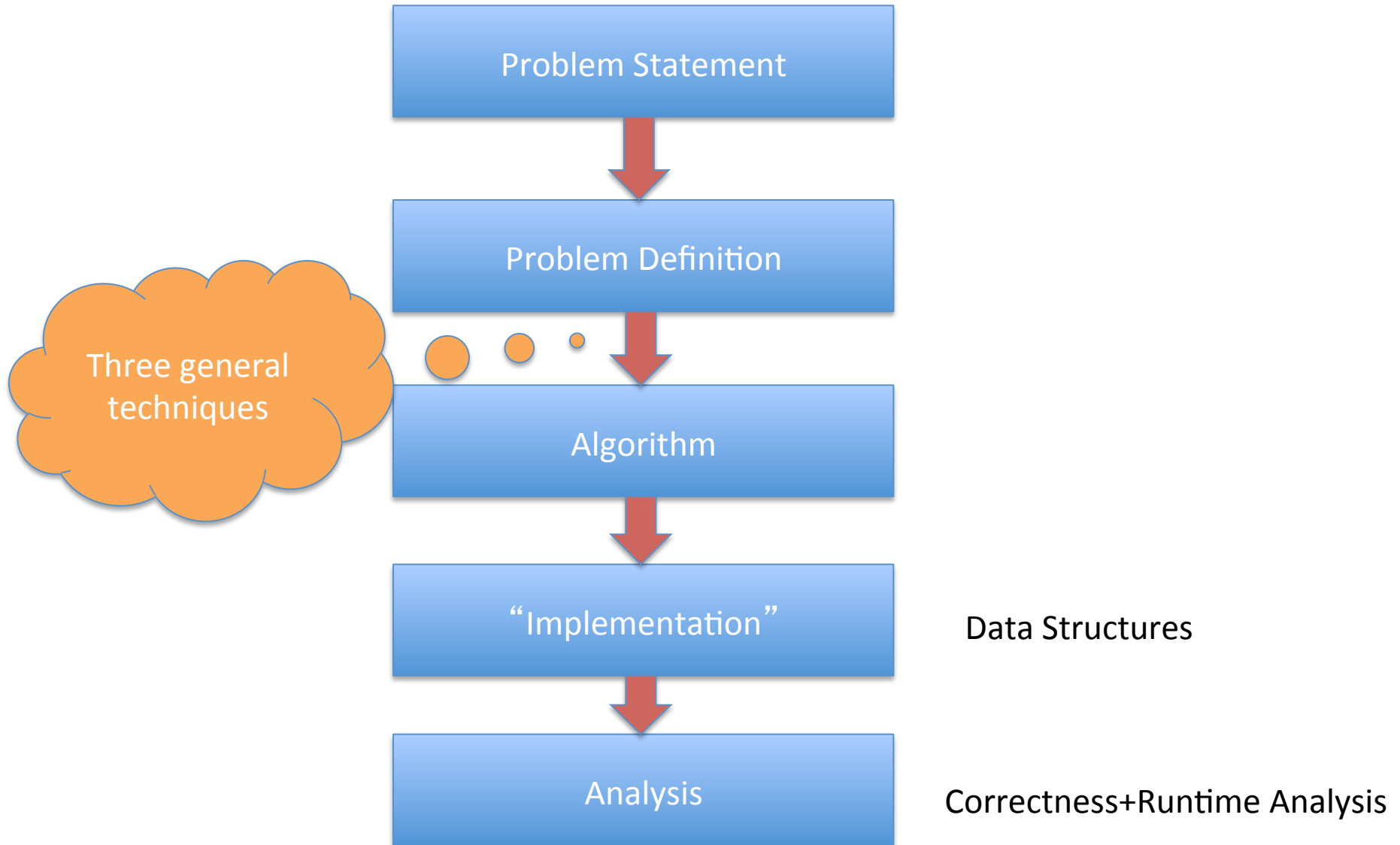
society

- An instructor (Atri Rudra) thinks this is a good note -

edit | undo good note | 2

Updated 9 hours ago by Tim Weppner

High level view of CSE 331



Greedy Algorithms

Natural algorithms



Reduced exponential running time to polynomial

Divide and Conquer

Recursive algorithmic paradigm



Reduced large polynomial time to smaller polynomial time

A new algorithmic technique

Dynamic Programming

Dynamic programming vs. Divide & Conquer



Same same because

Both design recursive algorithms



Different because

Dynamic programming is smarter about solving recursive sub-problems



End of Semester blues

Can only do one thing at any day: what is the optimal schedule to obtain maximum value?



Write up a term paper (10)

Party! (2)

Exam study (5)

331 HW (3)

Project (30)

Monday

Tuesday

Wednesday

Thursday

Friday

Previous Greedy algorithm

Order by end time and pick jobs greedily

Greedy value = $5+2+3=10$

Write up a term paper (10)

Party! (2)

Exam study (5)

331 HW (3)

Project (30)

OPT = 30

Monday

Tuesday

Wednesday

Thursday

Friday



Today's agenda

Formal definition of the problem

Start designing a recursive algorithm for the problem



Property of OPT

j in $\text{OPT}(j)$

j not in $\text{OPT}(j)$

$$\text{OPT}(j) = \max \{ v_j + \text{OPT}(p(j)), \text{OPT}(j-1) \}$$

Given $\text{OPT}(1), \dots, \text{OPT}(j-1)$,
how can one figure out if j
in optimal solution or not?



A recursive algorithm

Compute-Opt(j)

Correct for $j=0$

Proof of
correctness by
induction on j

If $j = 0$ then return 0

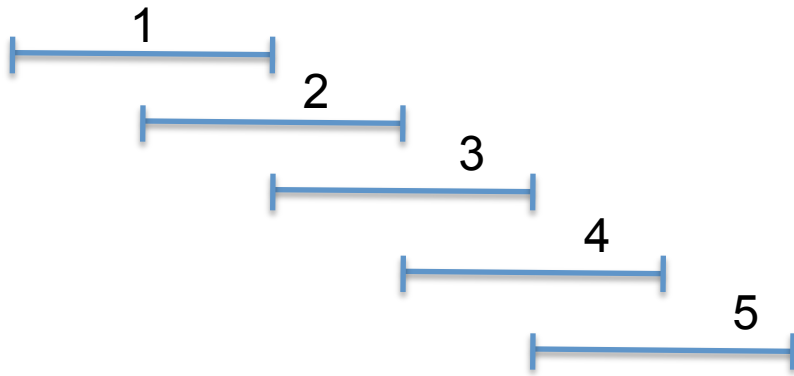
return $\max \{ v_j + \text{Compute-Opt}(p(j)), \text{Compute-Opt}(j-1) \}$

$= \text{OPT}(p(j))$

$= \text{OPT}(j-1)$

$$\text{OPT}(j) = \max \{ v_j + \text{OPT}(p(j)), \text{OPT}(j-1) \}$$

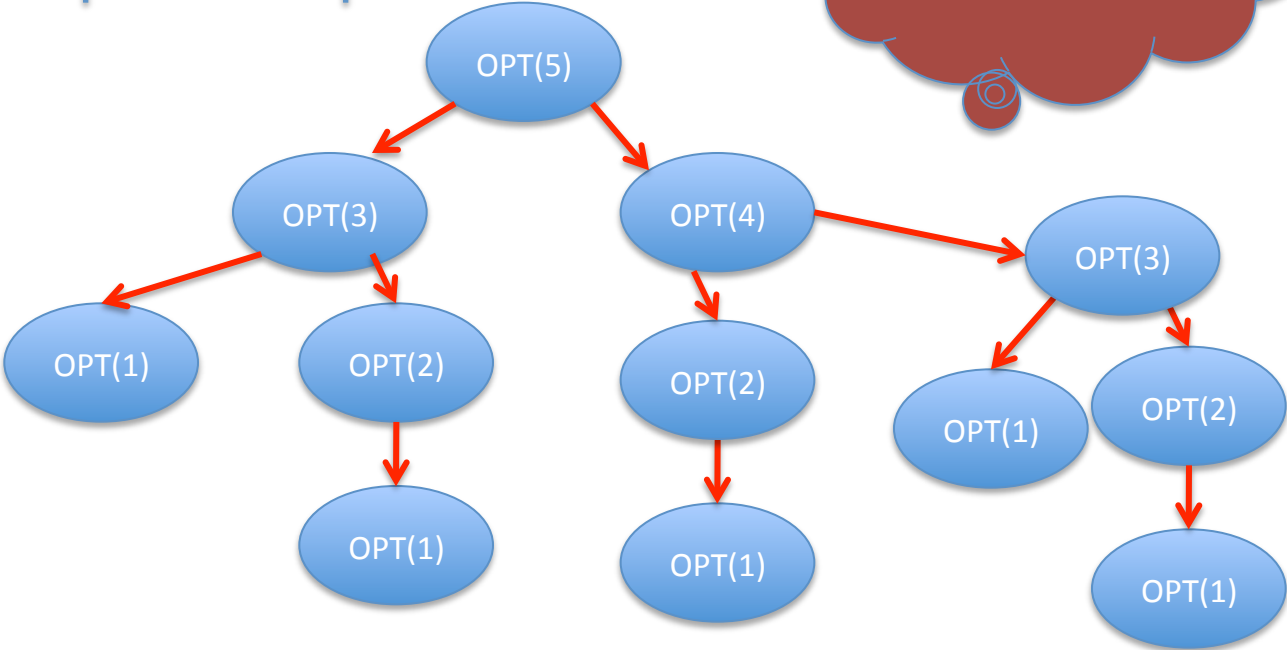
Exponential Running Time



$$p(j) = j - 2$$

Only 5 OPT values!

Formal proof: Ex.





How many distinct OPT values?

A recursive algorithm

M-Compute-Opt(j)

If $j = 0$ then return 0

If $M[j]$ is not null then return $M[j]$

$M[j] = \max \{ v_j + \text{M-Compute-Opt}(p(j)), \text{M-Compute-Opt}(j-1) \}$

return $M[j]$

M-Compute-Opt(j)
= OPT(j)

Run time = $O(\# \text{ recursive calls})$

Bounding # recursions

M-Compute-Opt(j)

If $j = 0$ then return 0

If $M[j]$ is not null then return $M[j]$

$M[j] = \max \{ v_j + \text{M-Compute-Opt}(p(j)), \text{M-Compute-Opt}(j-1) \}$

return $M[j]$

$O(n)$ overall

Whenever a recursive call is made an M value of assigned

At most n values of M can be assigned



Reading Assignment

Sec 6.1, 6.2 of [KT]



When to use Dynamic Programming

There are polynomially many sub-problems



Richard Bellman

Optimal solution can be computed from solutions to sub-problems

There is an ordering among sub-problem that allows for iterative solution