

Lecture 9

CSE 331

Sep 19, 2016

Mini Project choice due Sep 26

note ☆

0 views

Actions ▾

Mini project needs groups of size EXACTLY 3

A gentle reminder that your group composition is due in just over a week (11:59pm on Monday, Sep 26).

The important thing to note is that you need to send me **groups of size EXACTLY three**. This means you are responsible for finding two other students in 331 to form your group. I will **not** make any group assignments.

Feel free to use the comments on this post to try and find others who are still looking to form a group.

mini_project

good note | 0

Updated Just now by Airt Fluids

Gale-Shapley Algorithm

Initially all men and women are **free**

At most n^2 iterations

While there exists a free woman who can propose

Let w be such a woman and m be the best man she has not proposed to

w proposes to m

If m is free

(m,w) get **engaged**

Else (m,w') are engaged

If m prefers w' to w

w remains **free**

Else

(m,w) get **engaged** and w' is **free**

$O(1)$ time
implementation

Output the engaged pairs as the final output

Implementation Steps

(0) How to represent the input?

(1) How do we find a free woman w ?

(2) How would w pick her best unproposed man m ?

(3) How do we know who m is engaged to?

(4) How do we decide if m prefers w' to w ?

Overall running time

Init(1-4)



$n^2 \times (\text{Query/Update}(1-4))$

Questions?



Puzzle

Prove that **any** algorithm for the SMP takes $\Omega(n^2)$ time

Main Steps in Algorithm Design

Problem Statement



Problem Definition



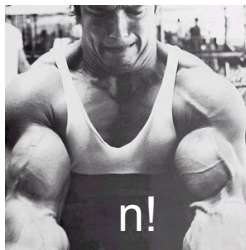
Algorithm



“Implementation”

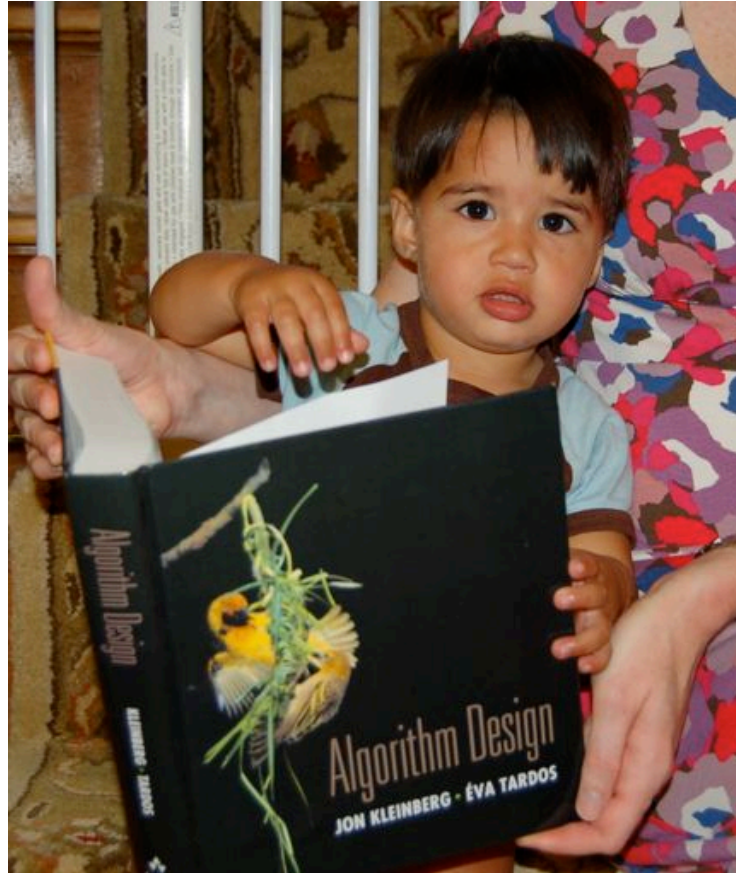


Analysis



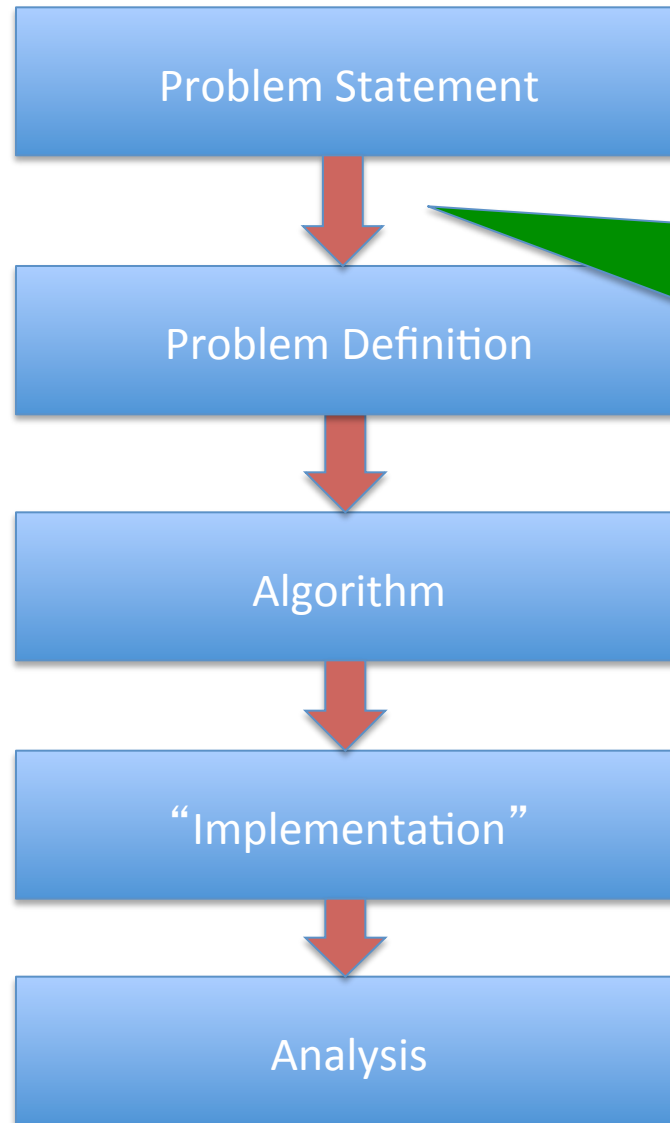
Correctness Analysis

Reading Assignments



Sec 1.1 and Chap. 2 in [KT]

Up Next....



A generic tool
to abstract
out problems

Graphs

Representation of relation

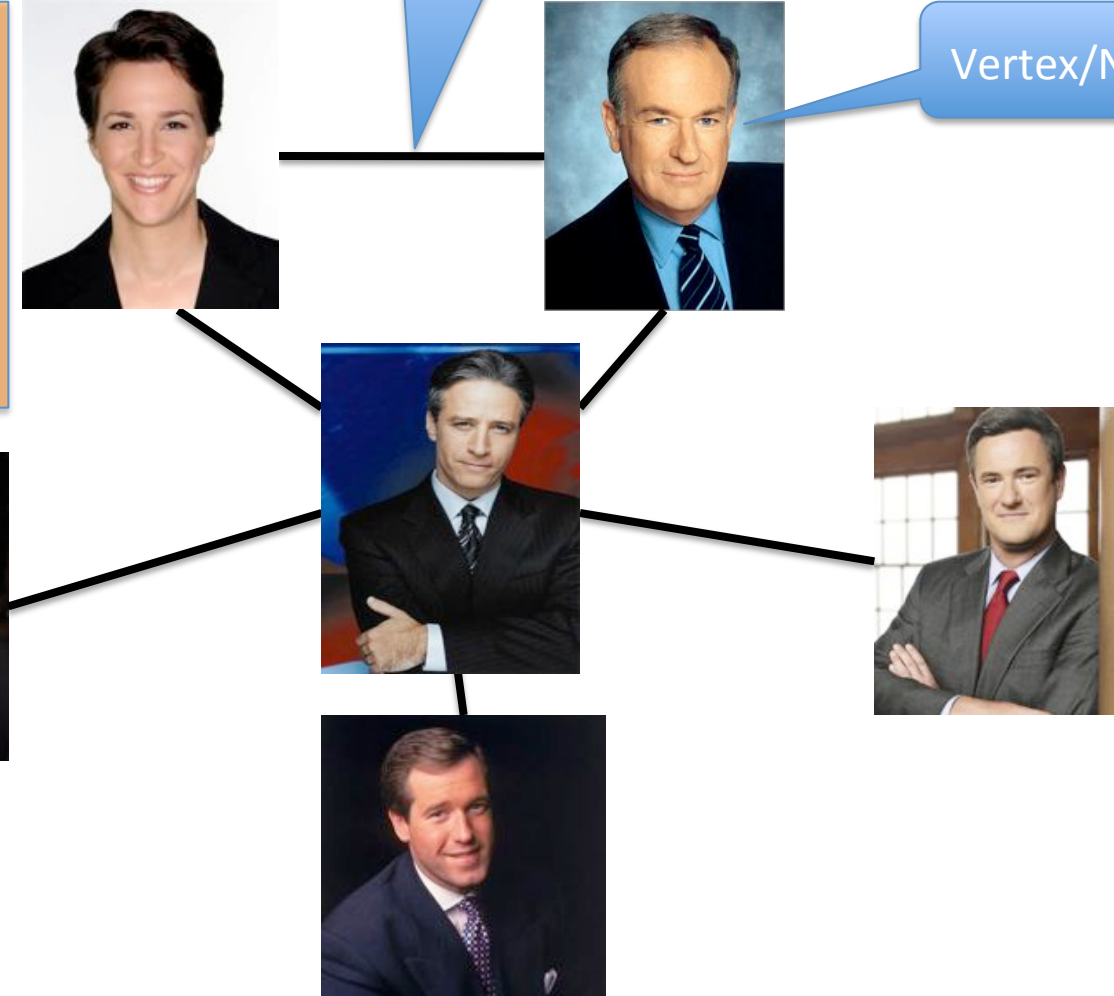
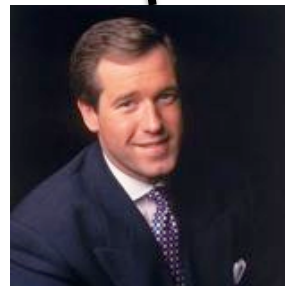
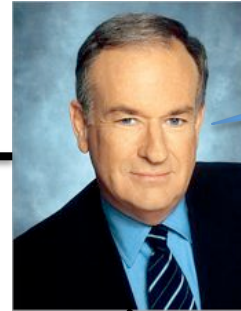
Edge

Pairs of entities/elements

Entities: News hosts

Relationship: Mention
in other's program

Vertex/Node



Graphs are omnipresent

Airline Route maps

jetBlue

HAPPY JETTING

Español • Help • Speak up

Book travel

Manage your flights

Travel deals

Where we jet

TrueBlue® program

Buffalo, NY [BUF]

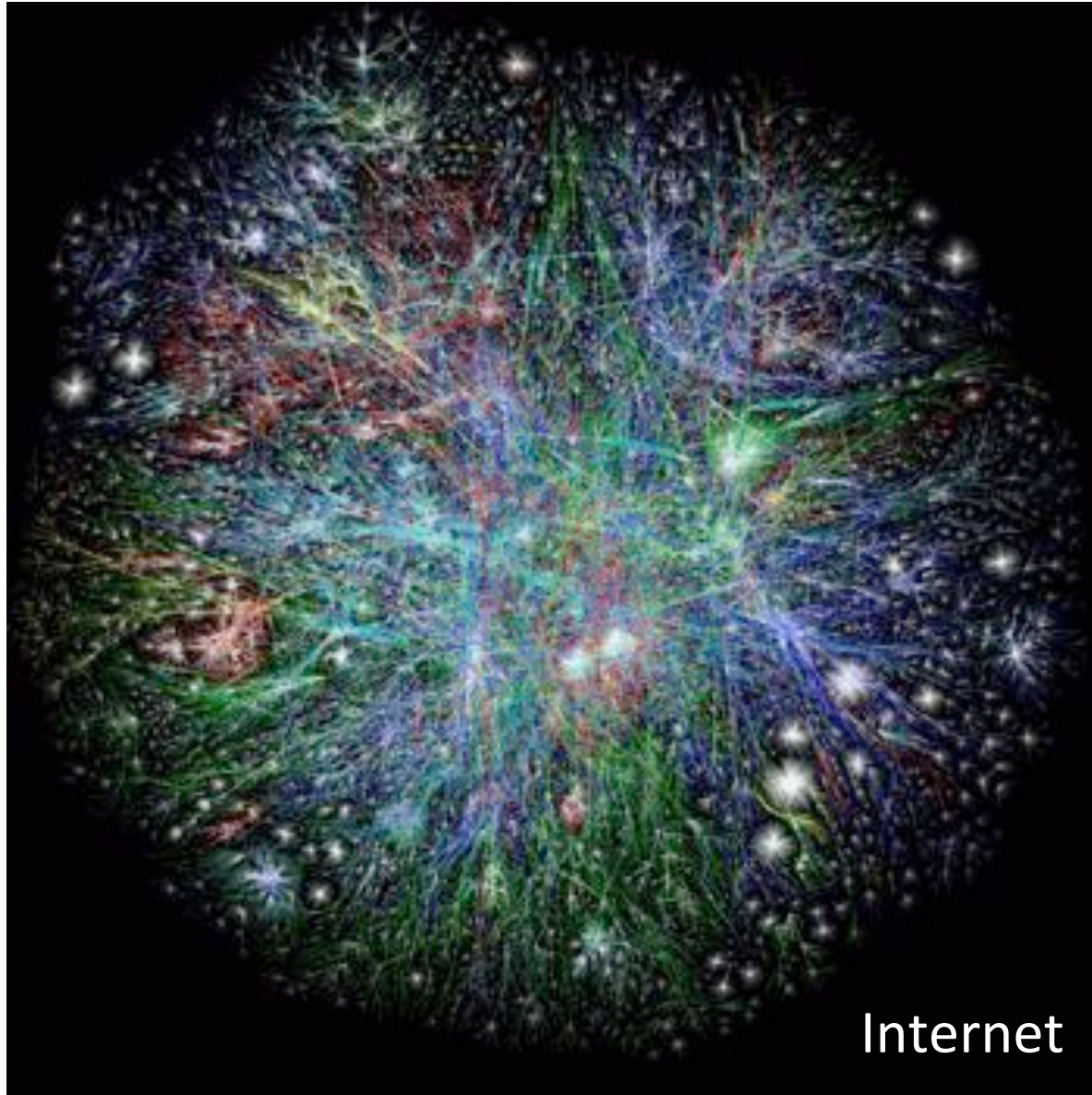
All Destinations

Nonstop Flights Only

Clear Map

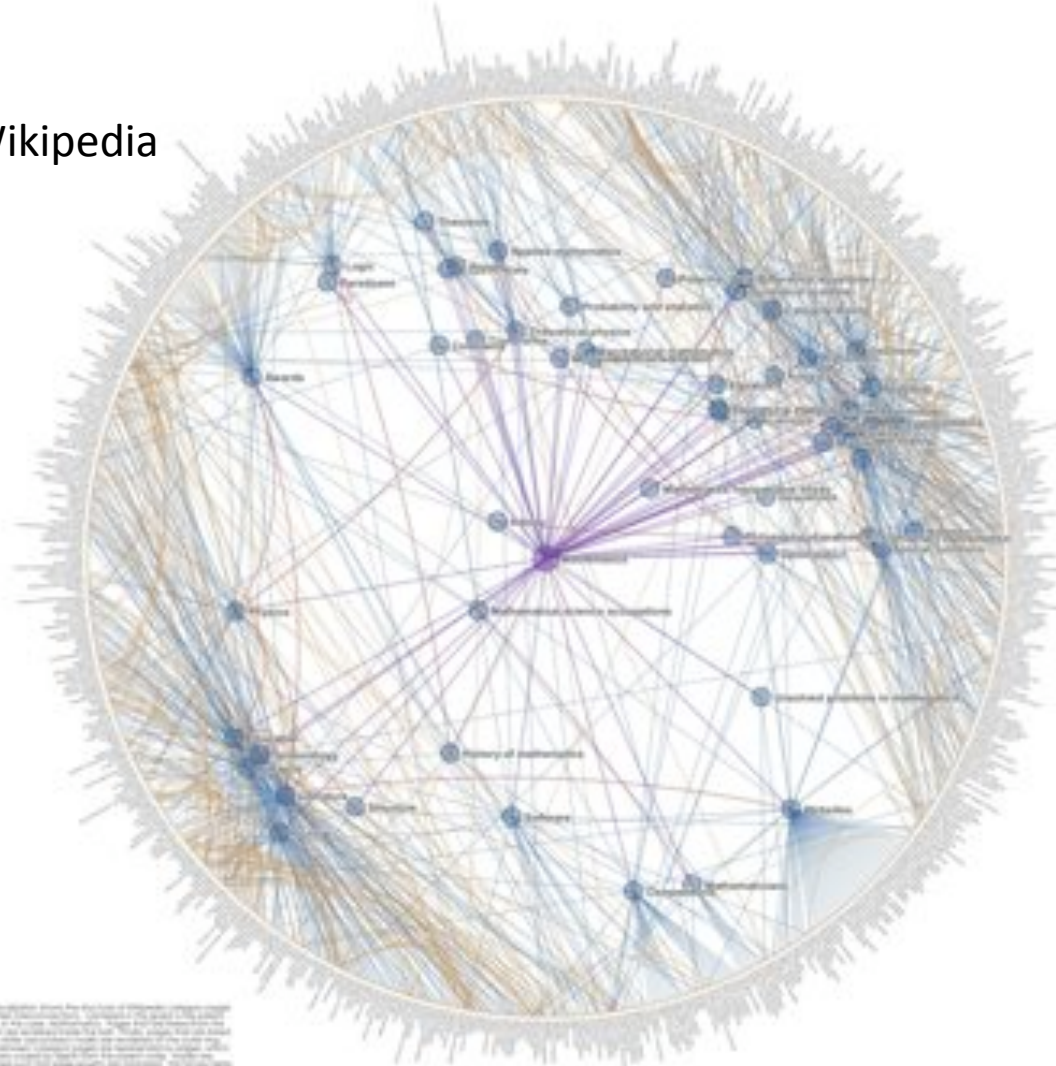


What does this graph represent?



And this one?

Math articles on Wikipedia



The visualization above is the result of a complex algorithm that takes as input a large number of articles from Wikipedia and outputs a network graph. The graph is a representation of the relationships between the articles, with nodes representing individual articles and edges representing connections between them. The color of the nodes and edges indicates the strength of the connections.

ChrisHarrison.net

© 2007 Chris Harrison

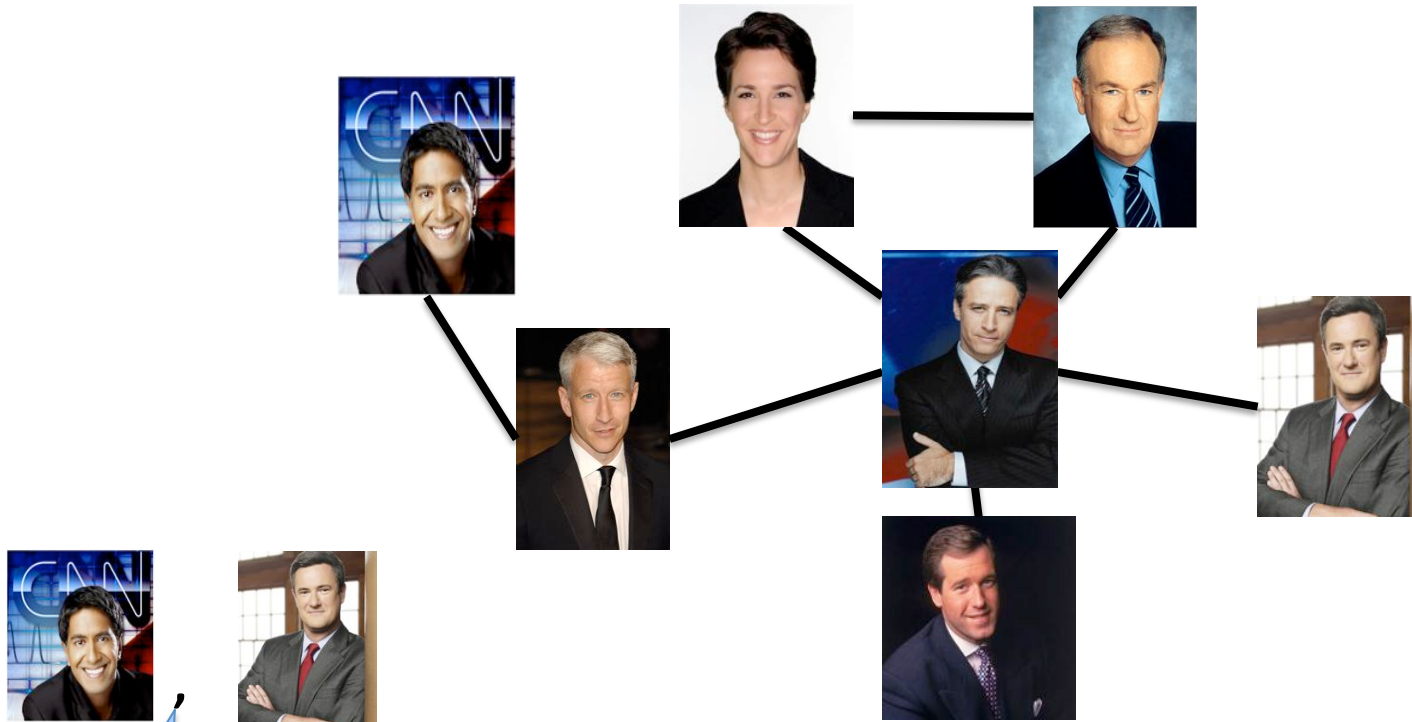
And this one?



Rest of today's agenda

Basic Graph definitions

Paths



Sequence of vertices connected by edges

Connected



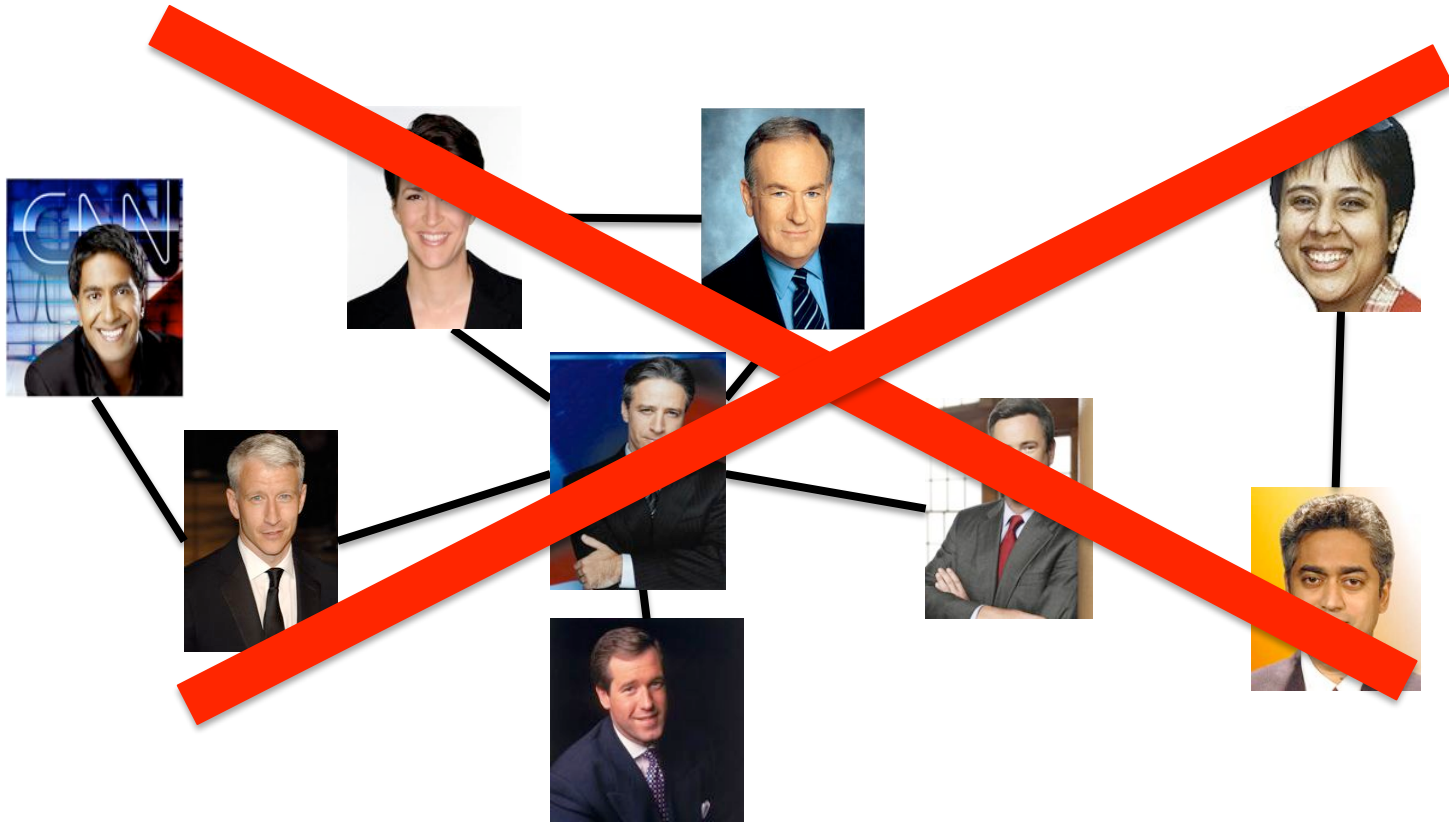
Path length 3

Connectivity

u and w are connected iff there is a path between them

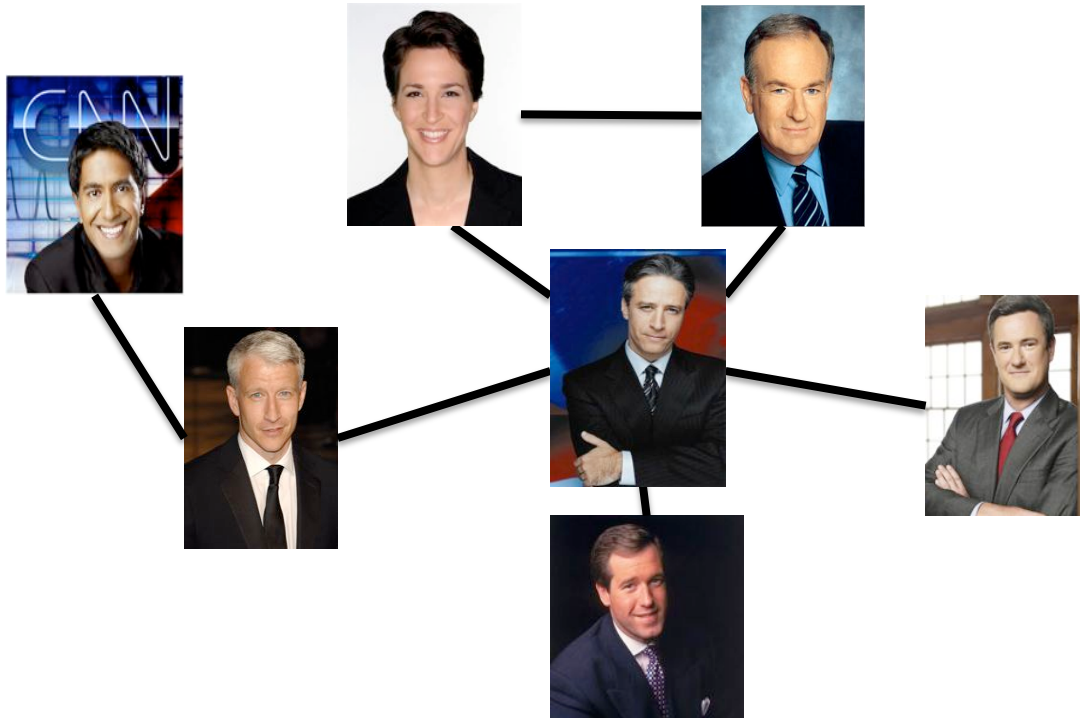
A graph is connected iff all pairs of vertices are connected

Connected Graphs



Every pair of vertices has a path between them

Cycles

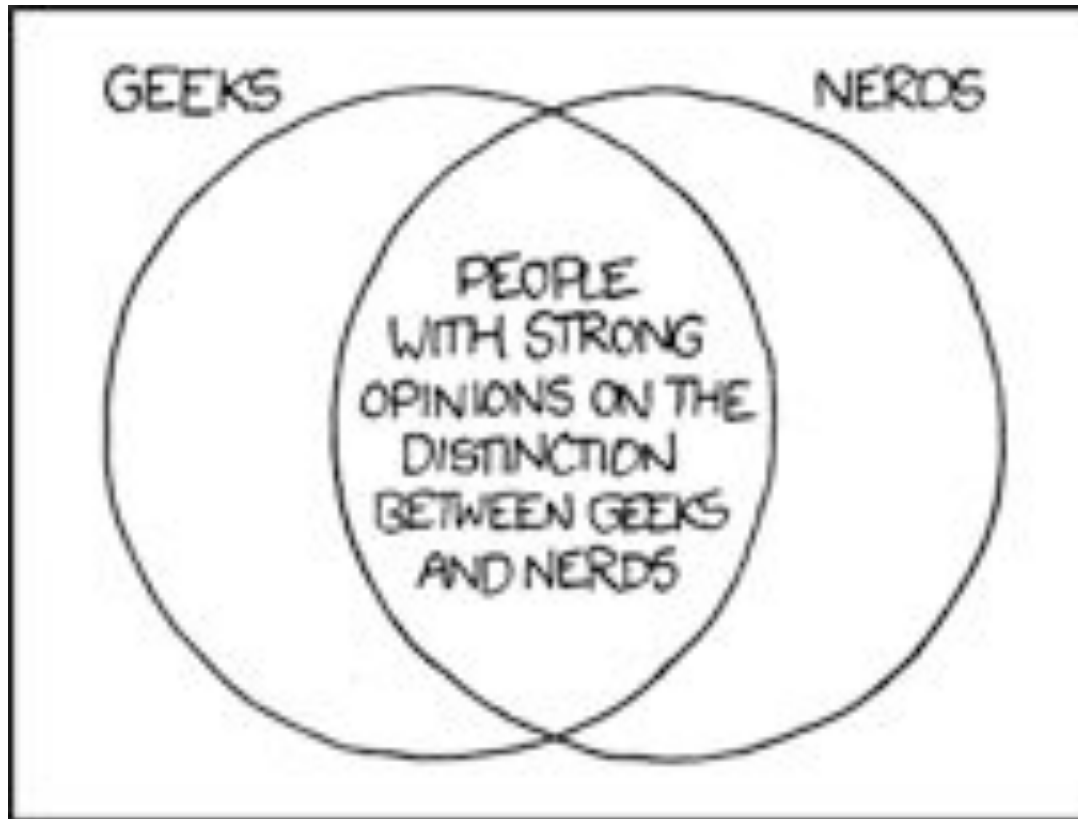


Sequence of k vertices connected by edges, first $k-1$ are distinct





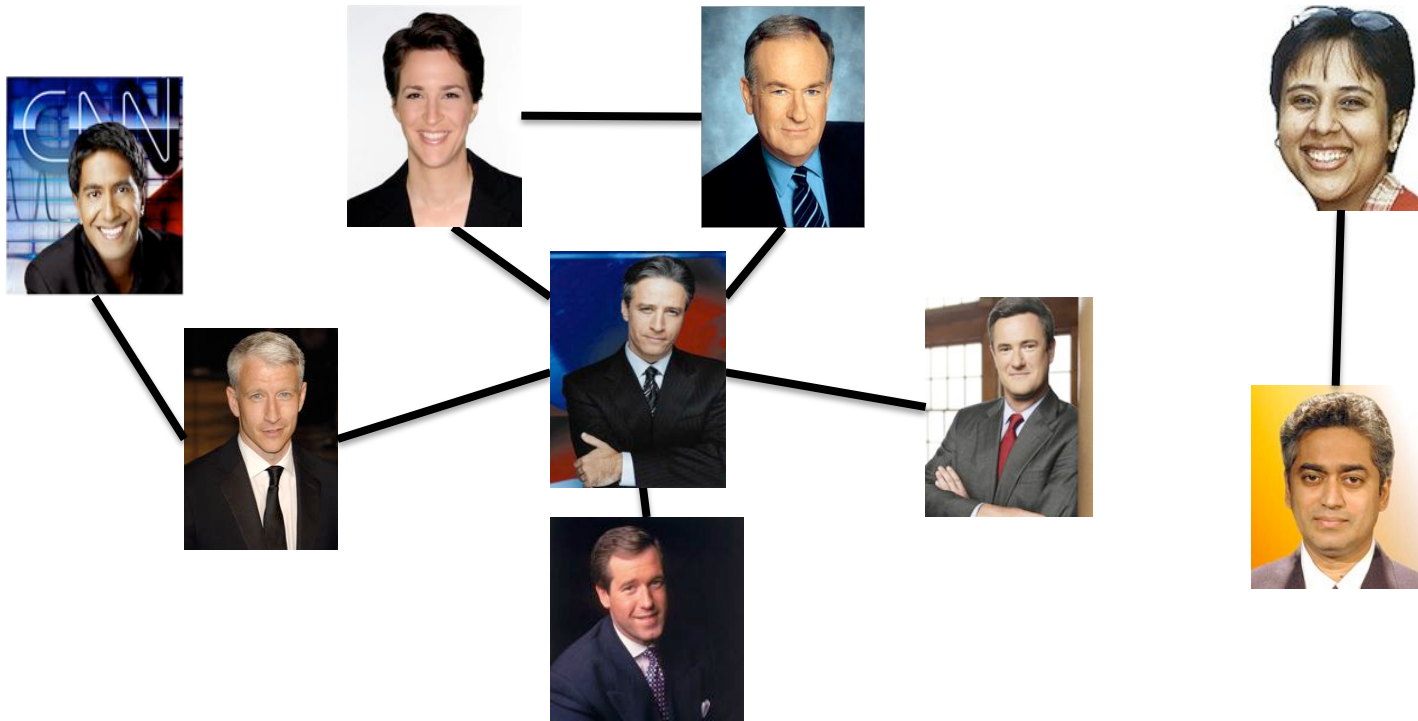
Formally define everything



http://imgs.xkcd.com/comics/geeks_and_nerds.png

Tree

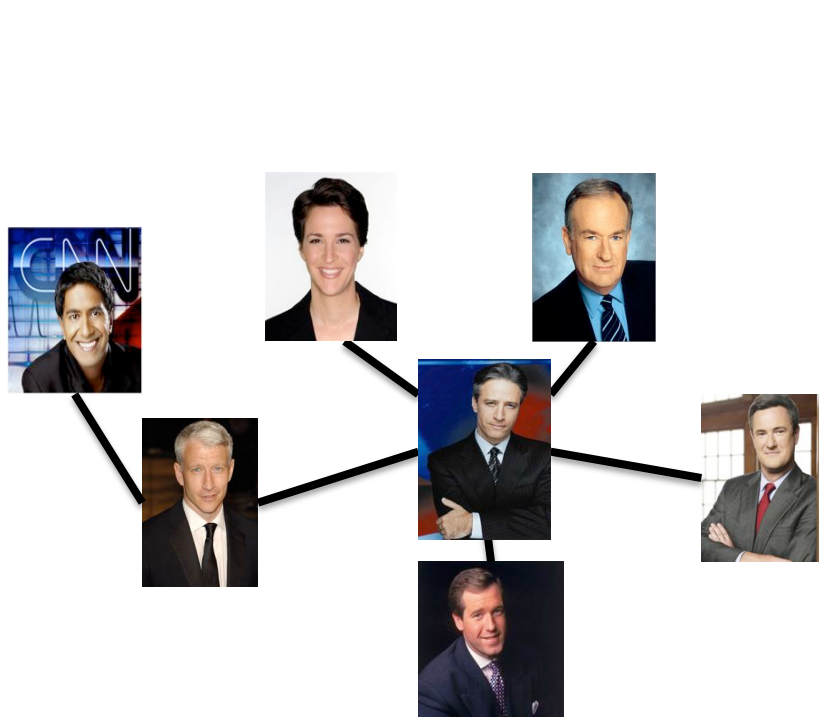
Connected undirected graph with no cycles



Rooted Tree

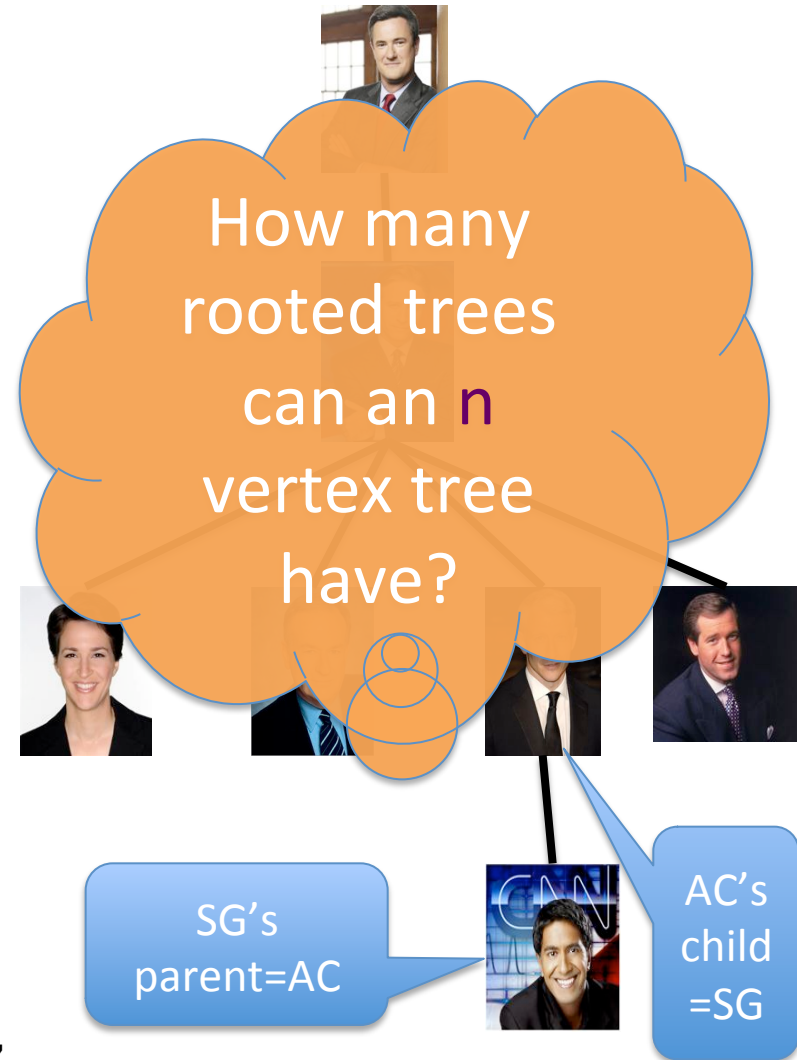


A rooted tree



Pick any vertex as root

Let the rest of the tree hang under “gravity”



Rest of Today's agenda

Prove n vertex tree has $n-1$ edges

Algorithms for checking connectivity