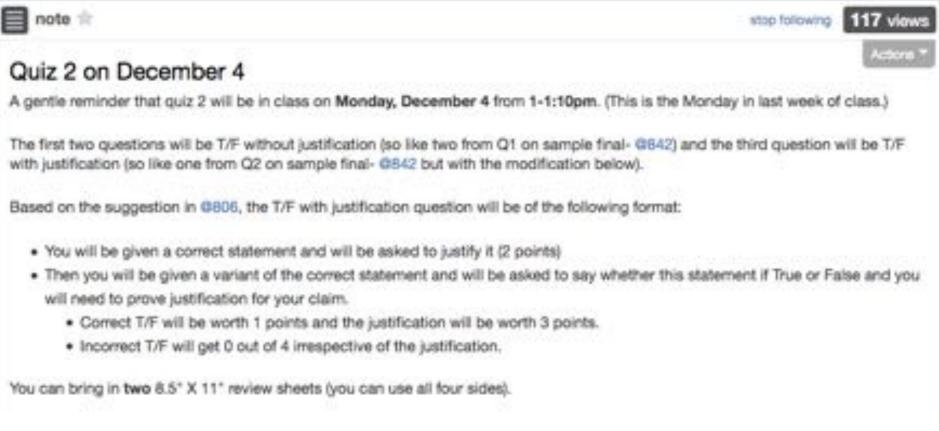
#### Lecture 37

CSE 331 Dec 1, 2017

# Quiz 2 on Monday



#### You can use two letter sized cheatsheets

# Last HW up!

## Homework 10

Due by 11:00am, Friday, December 8, 2017.

Make sure you follow all the homework policies.

All submissions should be done via Autolab.

#### Question 1 (Programming Assignment) [40 points]

#### <> Note:

This assignment can be solved in either Java, Python or C++ (you should pick the language you are most comfortable with). Please make sure to look at the supporting documentation and files for the language of your choosing.

#### The Problem

In this problem, you are given a directed graph (in adjacency list representation) G = (V, E) where each edge  $e \in E$  has cost  $c_e$  (which can be negative but G does not have a negative cost cycle) and a vertex  $s \in V$ . Your code will have to find the cost of shortest paths from s to every other node in V.

### HW 9 solutions

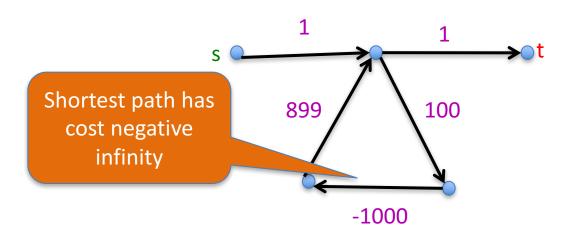
#### At the END of the lecture

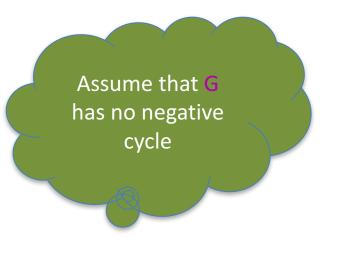
## Shortest Path Problem

Input: (Directed) Graph G=(V,E) and for every edge e has a cost  $c_e$  (can be <0)

t in V

Output: Shortest path from every s to t





#### When to use Dynamic Programming



There are polynomially many sub-problems

**Richard Bellman** 

Optimal solution can be computed from solutions to sub-problems

There is an ordering among sub-problem that allows for iterative solution

# Sub-problems

**OPT(u,i)** = cost of shortest path from u to t with at most i edges

# Today's agenda

Finish Bellman-Ford algorithm

Analyze the run time

### The recurrence

OPT(u,i) = shortest path from u to t with at most i edges

 $OPT(u,i) = min \{ OPT(u,i-1), min_{(u,w) in E} \{ c_{u,w} + OPT(w, i-1) \} \}$ 

#### Some consequences

**OPT(u,i)** = shortest path from u to t with at most i edges

 $OPT(u,i) = \min \left\{ OPT(u, i-1), \min_{(u,w) \text{ in } E} \left\{ c_{u,w} + OPT(w,i-1) \right\} \right\}$ 

OPT(u,n-1) is shortest path cost between u and t

Group talk time: How to compute the shortest path between s and t given all OPT(u,i) values

## Longest path problem

Given G, does there exist a simple path of length n-1?

### Longest vs Shortest Paths

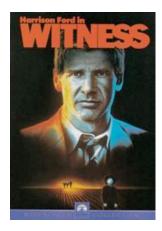


# Two sides of the "same" coin

Shortest Path problem

Can be solved by a polynomial time algorithm

Is there a longest path of length n-1?



Given a path can verify in polynomial time if the answer is yes

# Poly time algo for longest path?





#### **Clay Mathematics Institute**

Dedicated to increasing and disseminating mathematical knowledge

HOHE ABOUT CHE PROGRAMS NEWS & EVENTS AWARDS SCHOLARS PUBLICATIONS

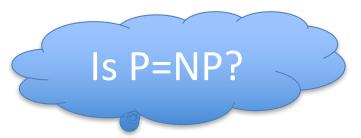
#### First Clay Mathematics Institute Millennium Prize Announced

Prize for Resolution of the Poincaré Conjecture Awarded to Dr. Grigoriy Perelman

- \* Birch and Swinnerton-Dver Conjecture
- Hodge Conjecture
- \* Navier-Stokes Equations
- P vs.NP
  Poincaré Conjecture
  - Longer & Andrews

### P vs NP question

 $\mathbf{P}$ : problems that can be solved by poly time algorithms



NP: problems that have polynomial time verifiable witness to optimal solution

Alternate NP definition: Guess witness and verify!

### Proving $P \neq NP$

Pick any one problem in NP and show it cannot be solved in poly time

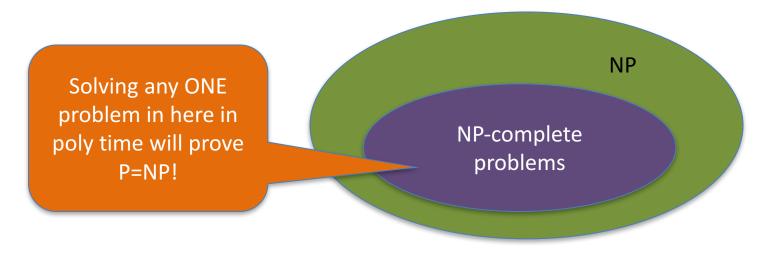
Pretty much all known proof techniques *provably* will not work

# Proving P = NP

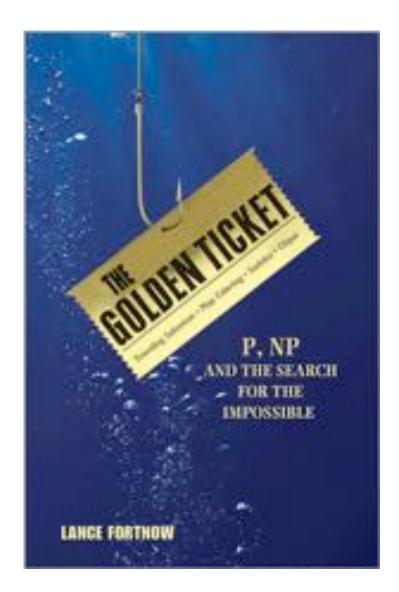
Will make cryptography collapse

Compute the encryption key!

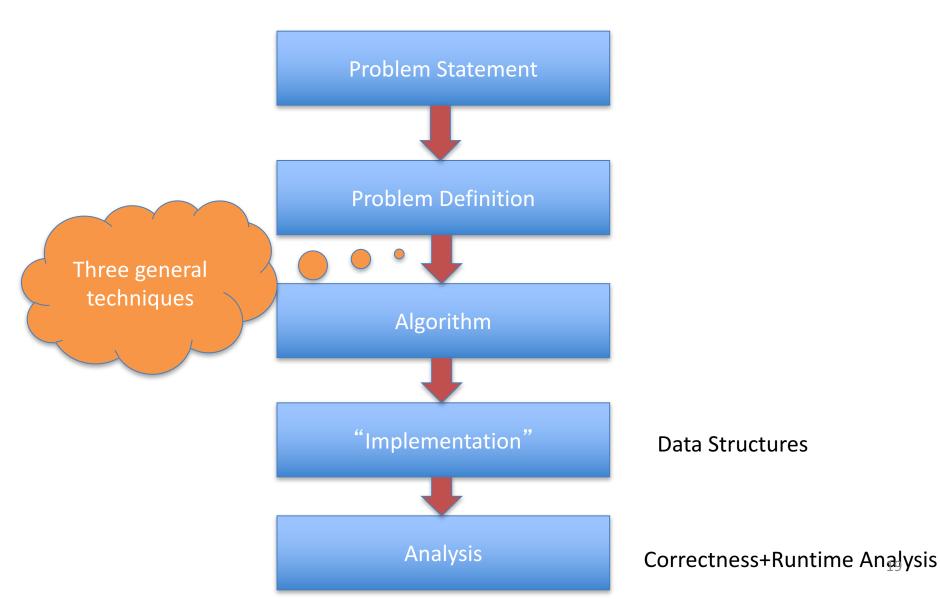
Prove that all problems in NP can be solved by polynomial time algorithms



### A book on P vs. NP



# High level view of CSE 331



# If you are curious for more

CSE 429 or 431: Algorithms

CSE 396: Theory of Computation

