

# Lecture 38

CSE 331

Dec 4, 2017

# Quiz 2

1:00-1:10pm

Lecture starts at 1:15pm

# Final Reminder

note ☆

stop following

147 views

Actions ▾

## Incentive for filling in the course evaluations

You must have received an email (or should be receiving an email shortly) about filling the course evaluation forms. I believe this is the link:

<https://www.smartevals.com/login.aspx?s=buffalo>

Here is my offer to incentivize you guys filling in the course evaluation form:

- If **at least 85%** of you fill in the course evaluation form, then I will release one T/F (without justification) question on the final exam (which corresponds to Q1(a): see @842 for the format).
- If **at least 95%** of you fill in the course evaluation form, then I will release one T/F (without justification) question and one T/F (with justification) question (corresponding to Q1(a) and Q2(a) respectively: see @842 for the format).

Of course if  $< 85\%$  of you fill in the course eval form, then no question gets released. I will post weekly updates on the response rate.

(Also to clarify: the % is only for students who are still registered in the course and have not resigned, which is an even 200.)

# Review sessions/extra OH

 poll ☆

stop following

19 views

Actions ▾

## Review sessions/extra OH

The final exam week will have one (or two-- depending on the response and room availability) review session(s) and Office hours hosted by the TAs. The review session(s) will be during Mon-Wed.

Copies of HW solutions can also be picked at the office hours.

Please choose all time slots that work for you (choose a slot even if it works only for part of the time).

**I will use the votes on Wed 8pm to pick the final slots.**

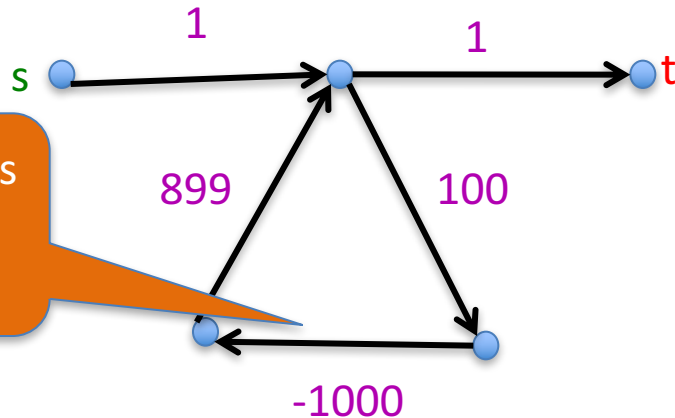
- Mon, Dec 11, 10-11am
- Mon, Dec 11, 11am -12pm
- Mon, Dec 11, 12-1pm
- Mon, Dec 11, 1-2pm
- Mon, Dec 11, 2-3pm
- Mon, Dec 11, 3-4pm
- Mon, Dec 11, 4-5pm

# Shortest Path Problem

Input: (Directed) Graph  $G=(V,E)$  and for every edge  $e$  has a cost  $c_e$  (can be  $<0$ )

$t$  in  $V$

Output: Shortest path from every  $s$  to  $t$



Shortest path has cost negative infinity

Assume that  $G$  has no negative cycle

# Longest path problem

Given  $G$ , does there exist a simple path of length  $n-1$  ?

# Longest vs Shortest Paths

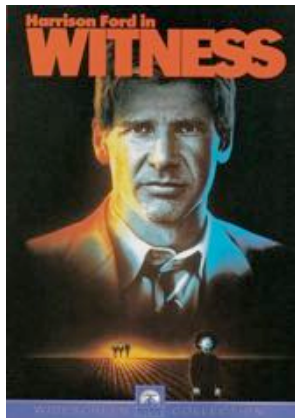


# Two sides of the “same” coin

Shortest Path problem

Can be solved by a polynomial time algorithm

Is there a longest path of length  $n-1$ ?



Given a path can verify in polynomial time if the answer is yes



# Poly time algo for longest path?



## Clay Mathematics Institute

*Dedicated to increasing and disseminating mathematical knowledge*

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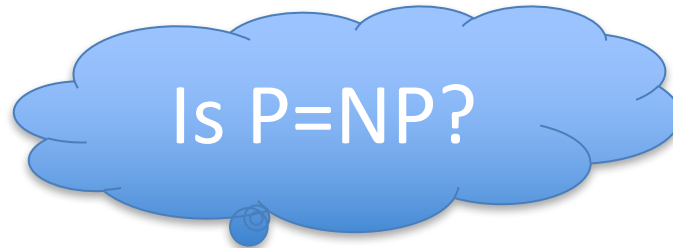
### First Clay Mathematics Institute Millennium Prize Announced

Prize for Resolution of the Poincaré Conjecture Awarded to Dr. Grigoriy Perelman

- Birch and Swinnerton-Dyer Conjecture
- Hodge Conjecture
- Navier-Stokes Equations
- P vs NP
- Poincaré Conjecture
- Riemann Hypothesis

# P vs NP question

**P**: problems that can be solved by poly time algorithms

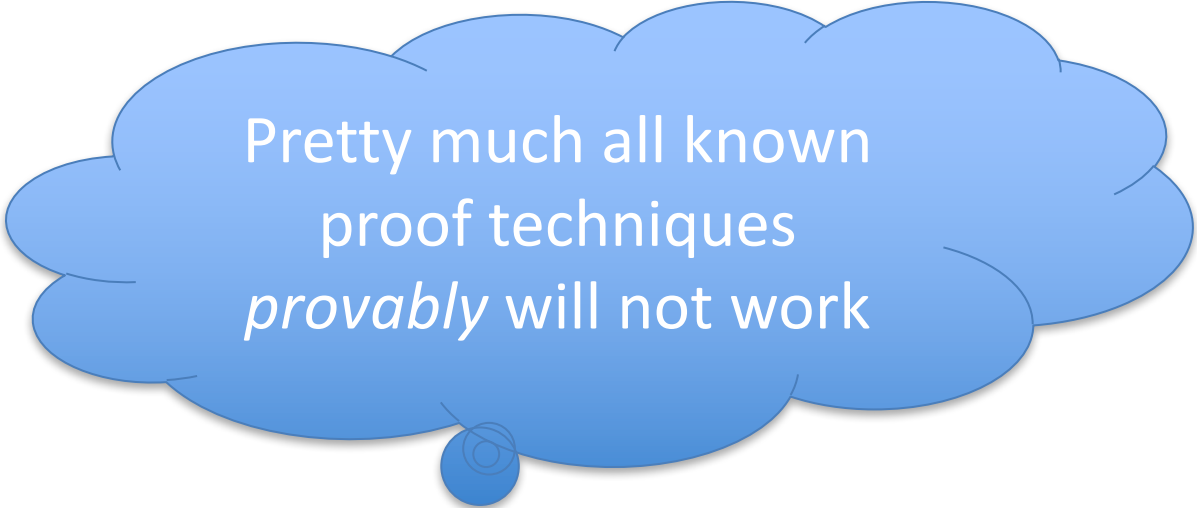


**NP**: problems that have polynomial time verifiable witness to optimal solution

Alternate NP definition: Guess witness and verify!

# Proving $P \neq NP$

Pick any one problem in NP and show it cannot be solved in poly time



Pretty much all known  
proof techniques  
*provably* will not work

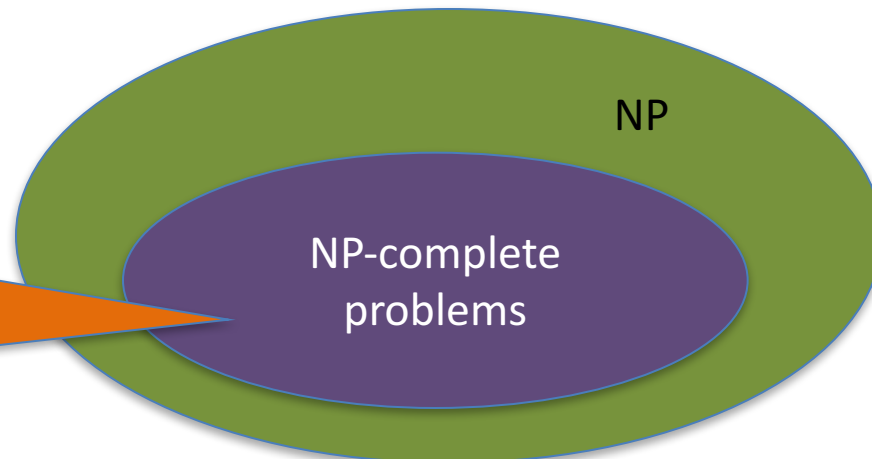
# Proving $P = NP$

Will make cryptography collapse

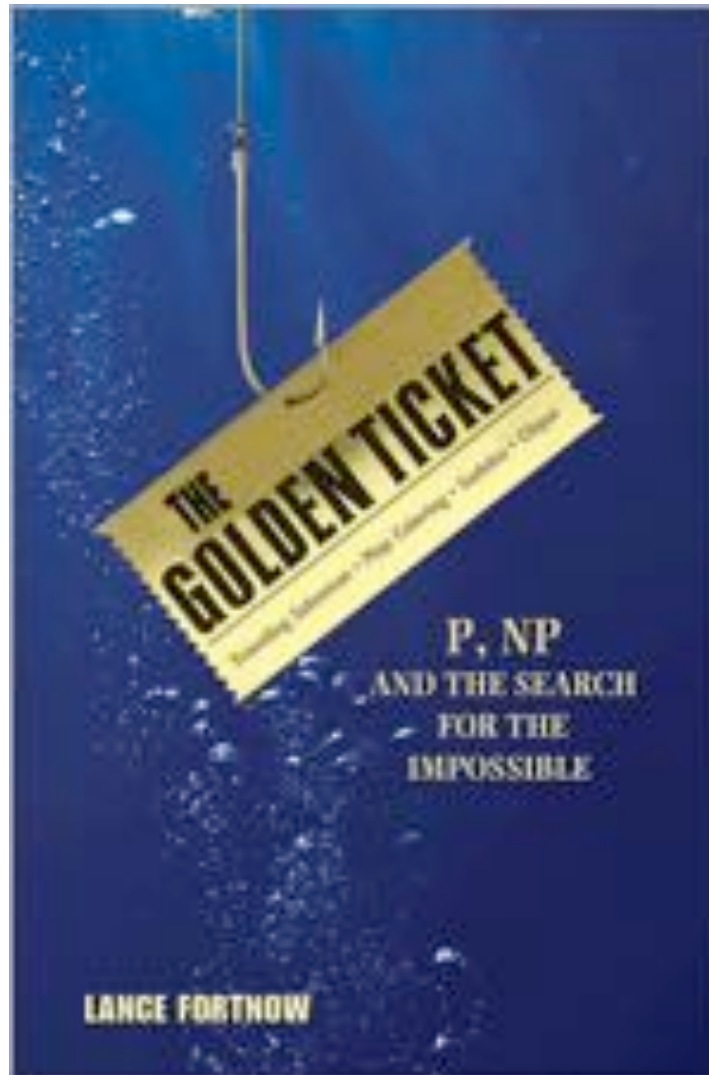
Compute the encryption key!

Prove that all problems in NP can be solved by polynomial time algorithms

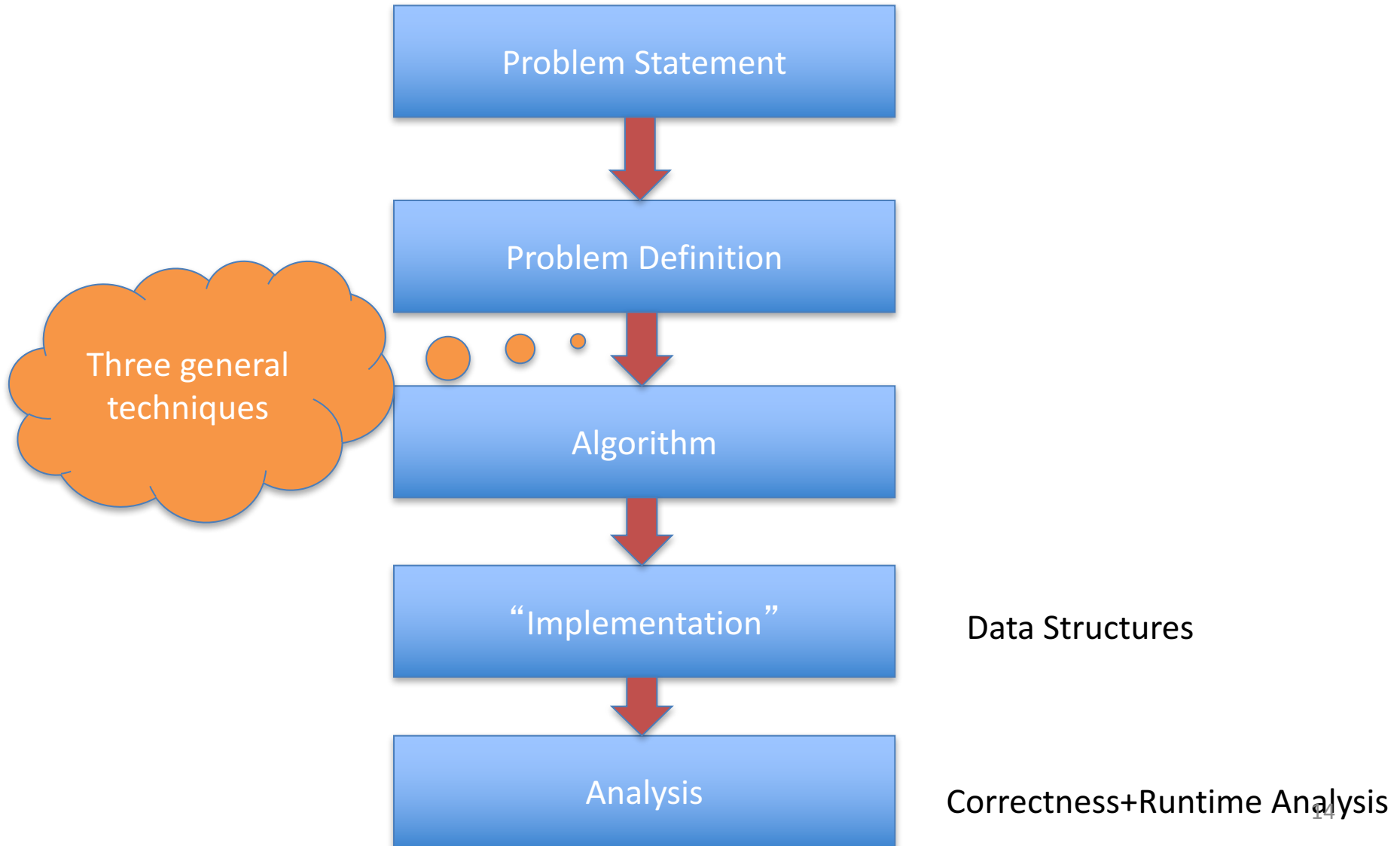
Solving any ONE problem in here in poly time will prove  $P=NP!$



# A book on P vs. NP



# High level view of CSE 331



# If you are curious for more

CSE 429 or 431: Algorithms

CSE 396: Theory of Computation



Now relax...





# Randomized algorithms

## What is different?

Algorithms can toss coins and make decisions

## A Representative Problem

Hashing

## Further Reading

Chapter 13 of the textbook



<http://calculator.mathcaptain.com/coin-toss-probability-calculator.html>



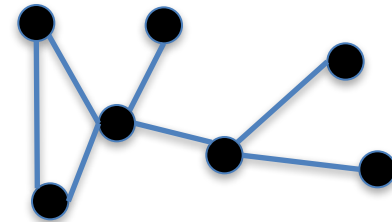
# Approximation algorithms

## What is different?

Algorithms can output a solution that is say 50% as good as the optimal

## A Representative Problem

Vertex Cover



## Further Reading

Chapter 12 of the textbook



# Online algorithms

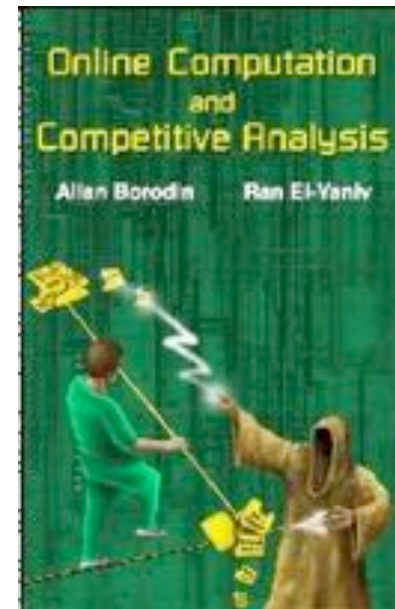
## What is different?

Algorithms have to make decisions before they see all the input

## A Representative Problem

Secretary Problem

## Further Reading



# Data streaming algorithms

What is different?



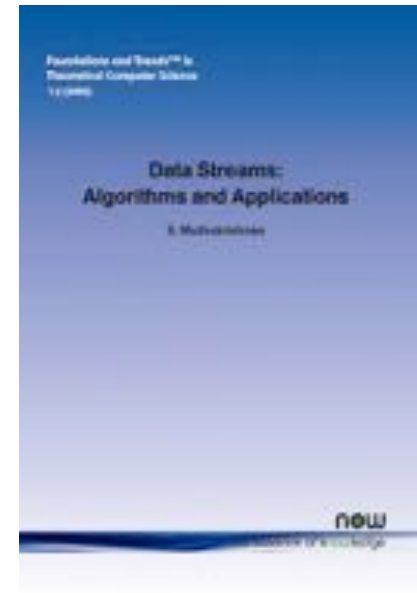
<https://www.flickr.com/photos/midom/2134991985/>

One pass on the input with severely limited memory

## A Representative Problem

Compute the top-10 source IP addresses

## Further Reading



# Distributed algorithms

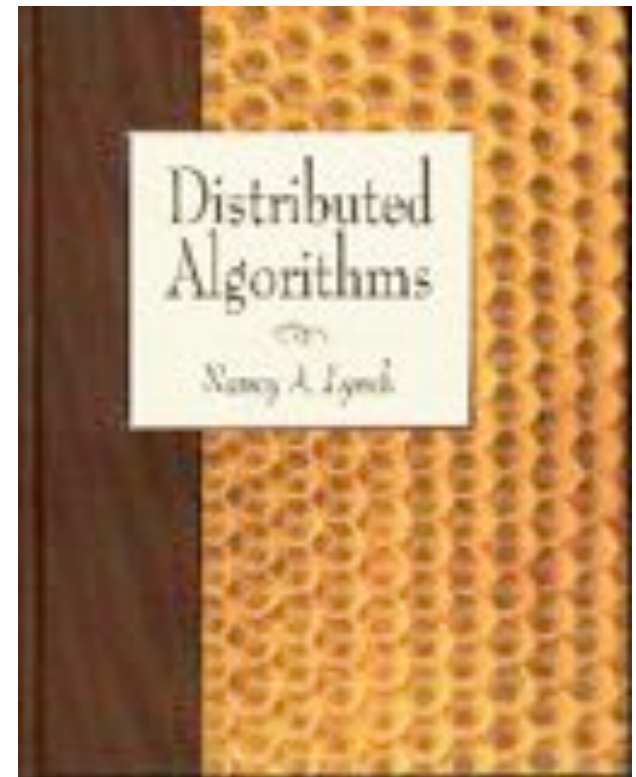
What is different?

Input is distributed over a network

A Representative Problem

Consensus

Further Reading



# Beyond-worst case analysis

## What is different?

Analyze algorithms in a more instance specific way

## A Representative Problem

Intersect two sorted sets

## Further Reading



<http://theory.stanford.edu/~tim/f14/f14.html>

# Algorithms for Data Science

What is different?

Algorithms for non-discrete inputs

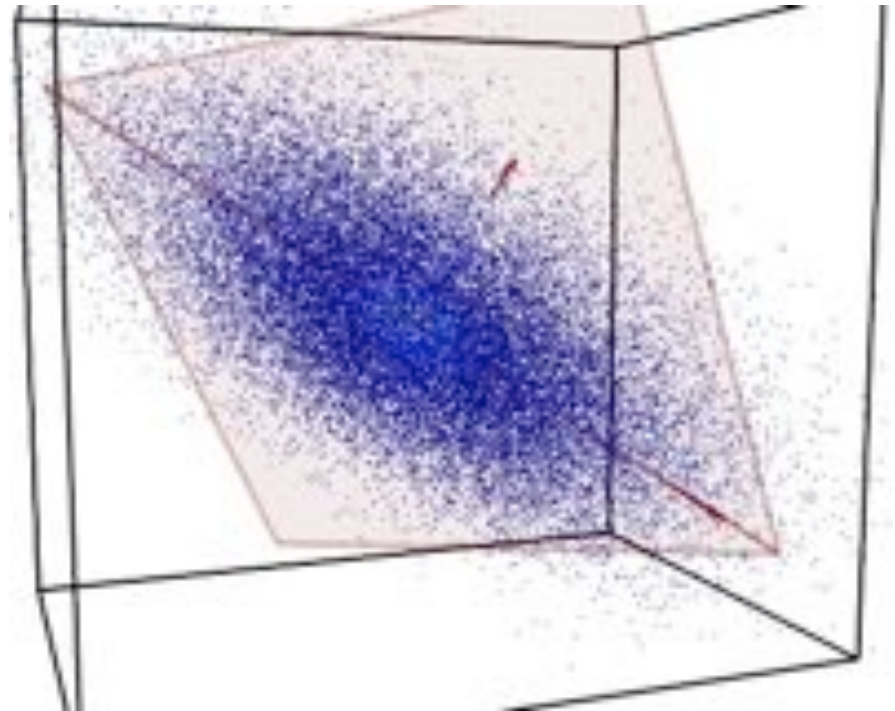
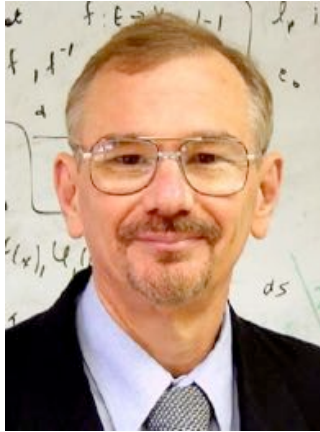
A Representative Problem

Compute Eigenvalues

Further Reading

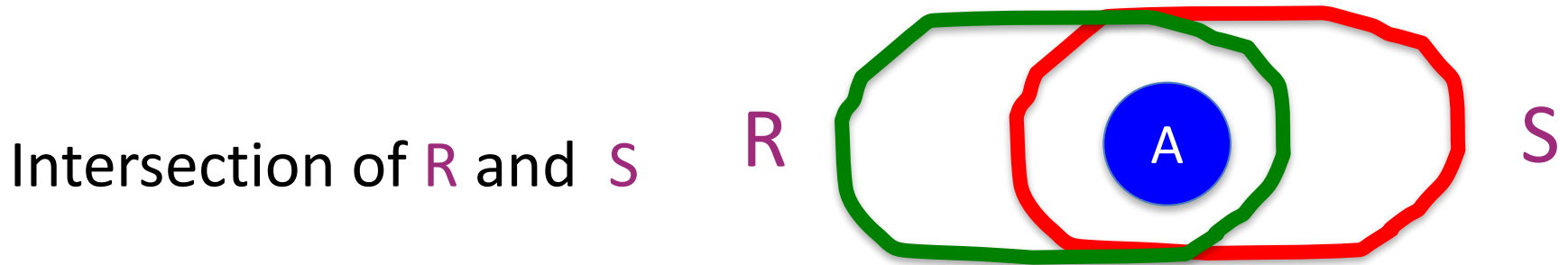


# Johnson Lindenstrauss Lemma





# The simplest non-trivial join query

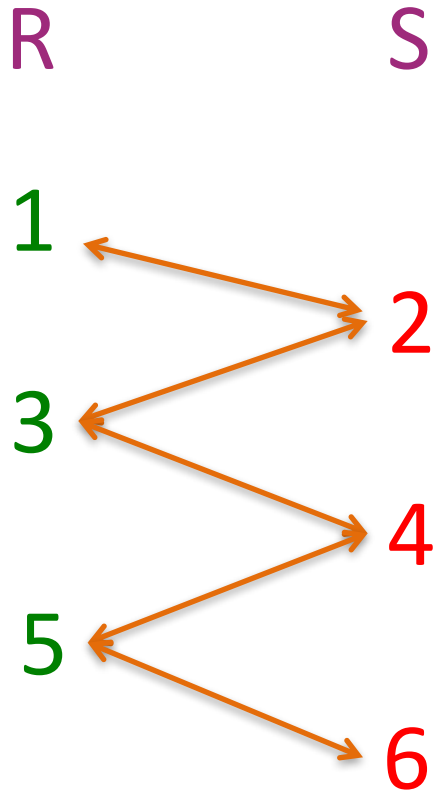


Assume  $R$  and  $S$  are sorted

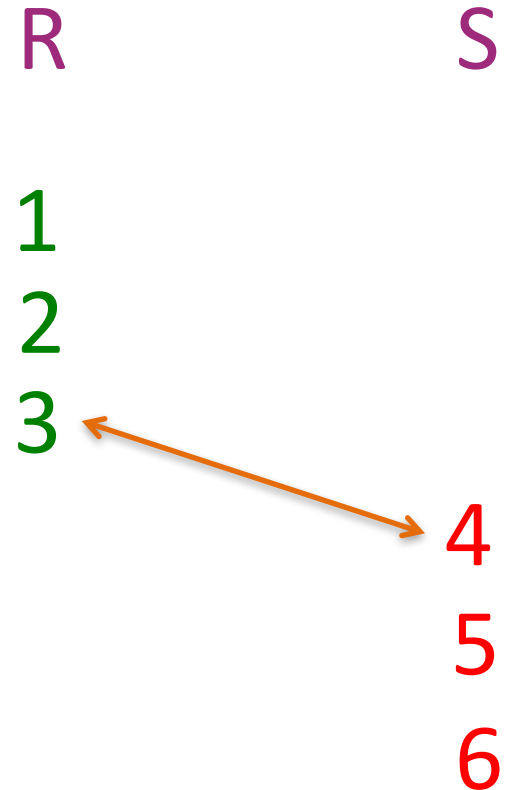
Let us concentrate on comparison based algorithms

Assume  $|R| = |S| = N$

# Not all inputs are created equal



$\Omega(N)$  comparisons

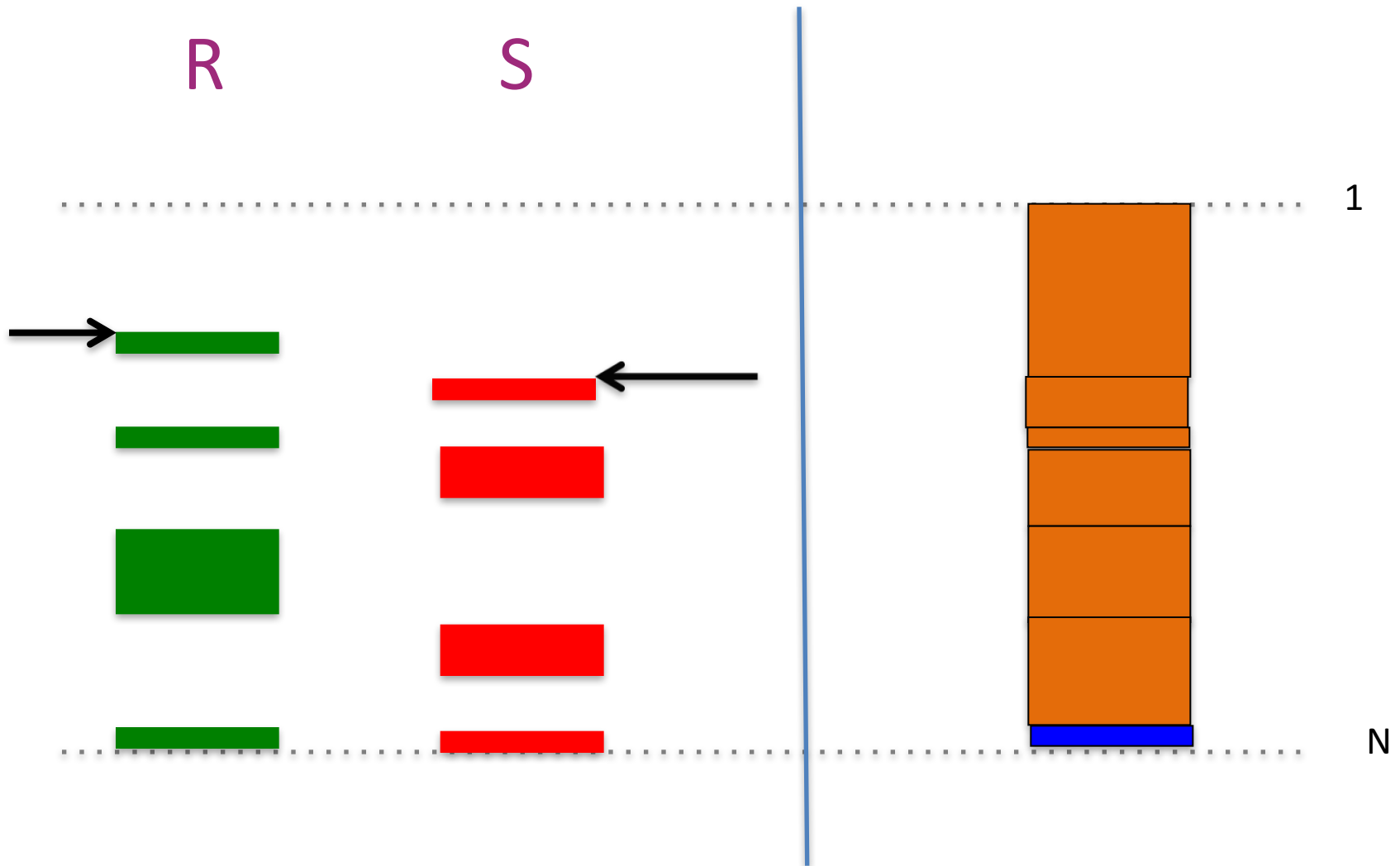


1 comparison!

We need a faster/adaptive algorithm



# The MERGE algorithm works



# An assumption

Output of the join is empty

# MERGE is (near) instance optimal

Benchmark: Minimum number of comparisons ( $C$ ) to “certify” output



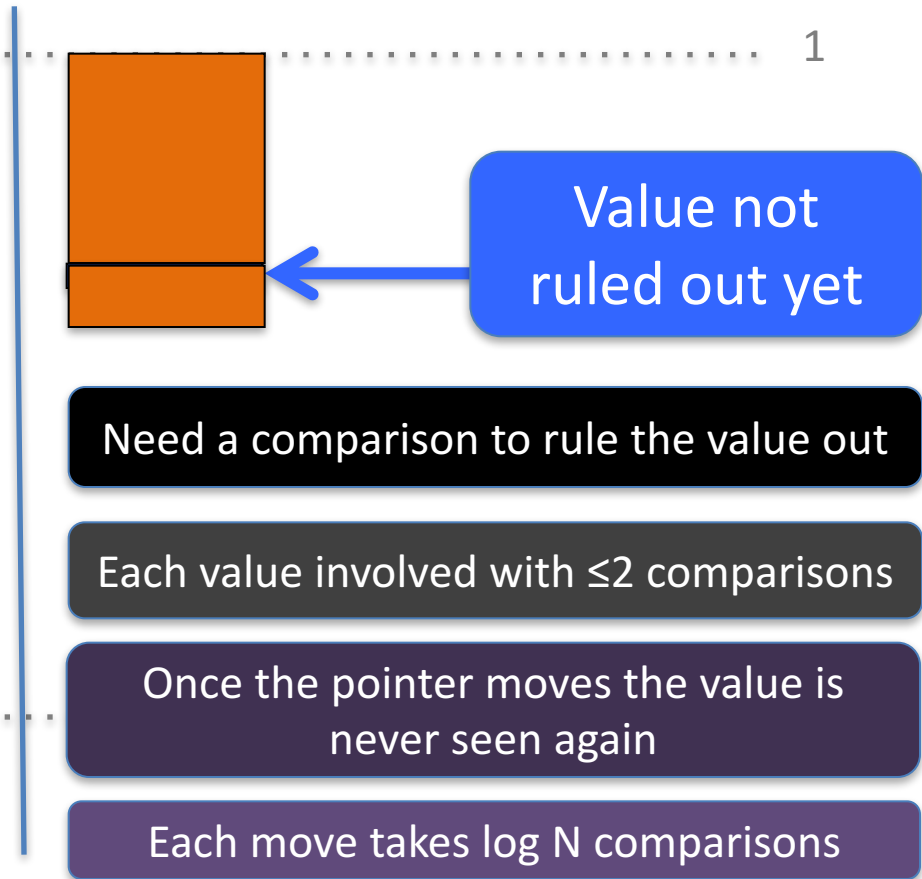
Demaine

Lopez-Ortiz

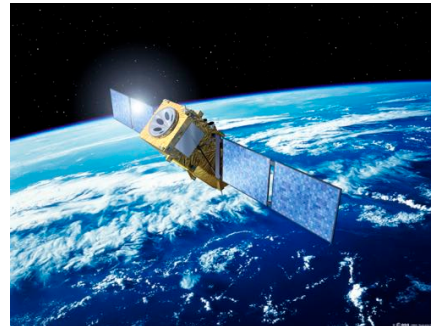
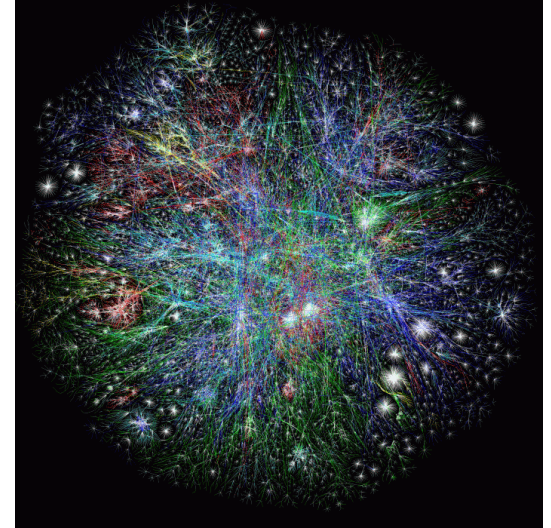
Munro

$C \log N$   
comparisons  
(and time)

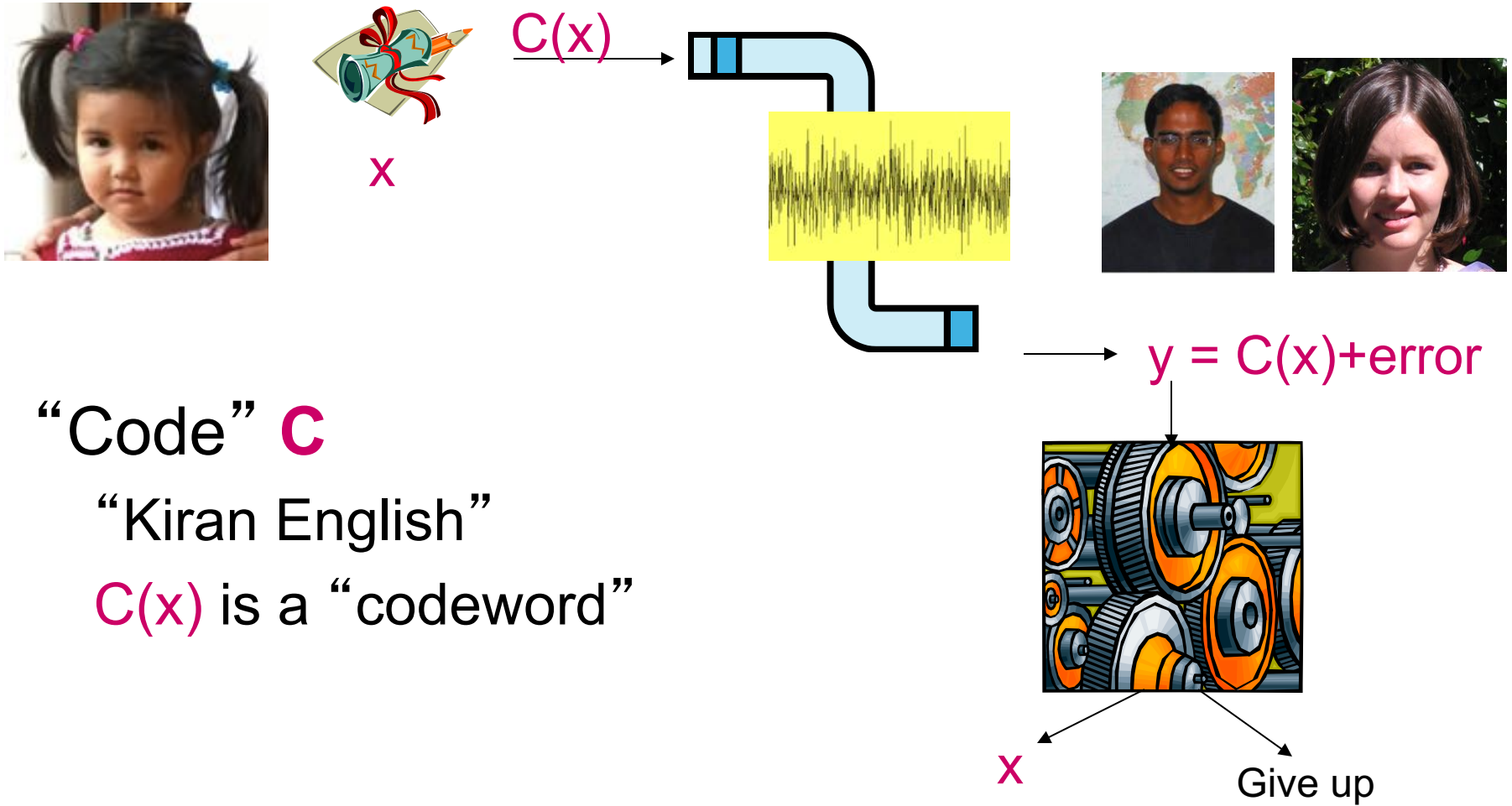
R S



# Coding Theory



# Communicating with my 3 year old



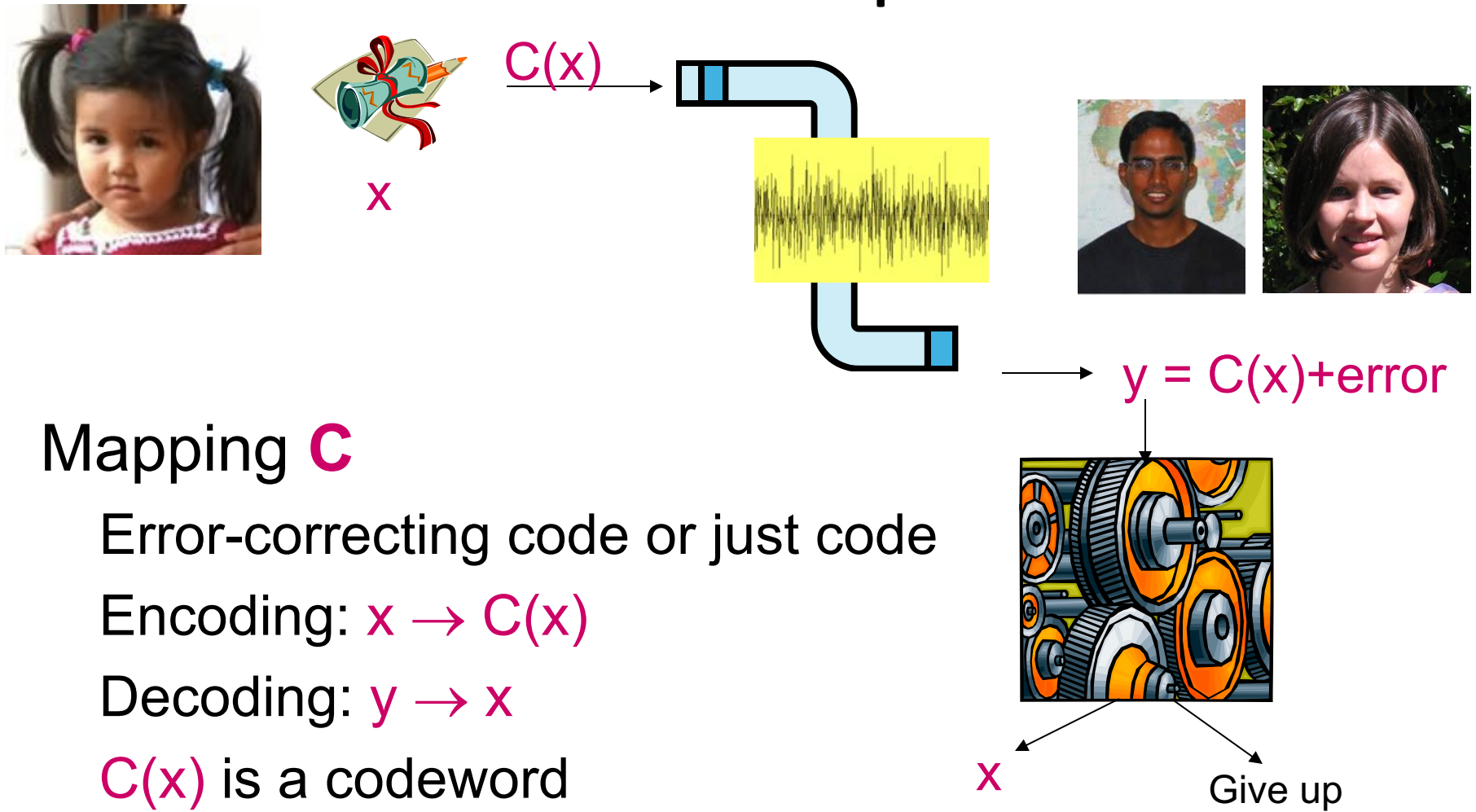
“Code” **C**

“Kiran English”

**C(x)** is a “codeword”



# The setup



## Mapping $C$

Error-correcting code or just code

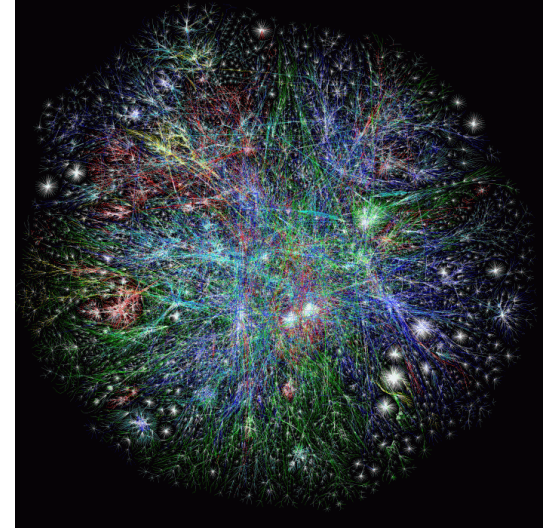
Encoding:  $x \rightarrow C(x)$

Decoding:  $y \rightarrow x$

$C(x)$  is a codeword

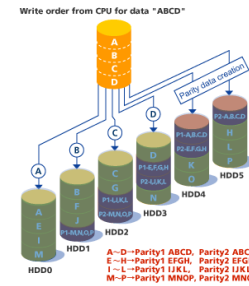
# Different Channels and Codes

- Internet
  - Checksum used in mult layers of TCP/IP stack
- Cell phones
- Satellite broadcast
  - TV
- Deep space telecommunications
  - Mars Rover

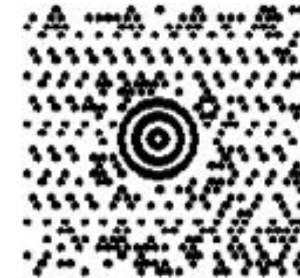


# “Unusual” Channels

- Data Storage
  - CDs and DVDs
  - RAID
  - ECC memory



- Paper bar codes
  - UPS (MaxiCode)



Codes are all around us

# Redundancy vs. Error-correction

- **Repetition code**: Repeat every bit say 100 times
  - Good error correcting properties
  - Too much redundancy
- **Parity code**: Add a parity bit
  - Minimum amount of redundancy
  - Bad error correcting properties
    - Two errors go completely undetected
- Neither of these codes are satisfactory

1 1 1 0 0	1
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1 0 0 0 0	1
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# Two main challenges in coding theory

- Problem with parity example
  - Messages mapped to codewords which do not differ in many places
- Need to pick a lot of codewords that differ a lot from each other
- Efficient decoding
  - Naive algorithm: check received word with all codewords

# The fundamental tradeoff

- Correct as **many errors** as possible with as **little redundancy** as possible

Can one achieve the “optimal” tradeoff with *efficient* encoding and decoding ?

Interested in more?

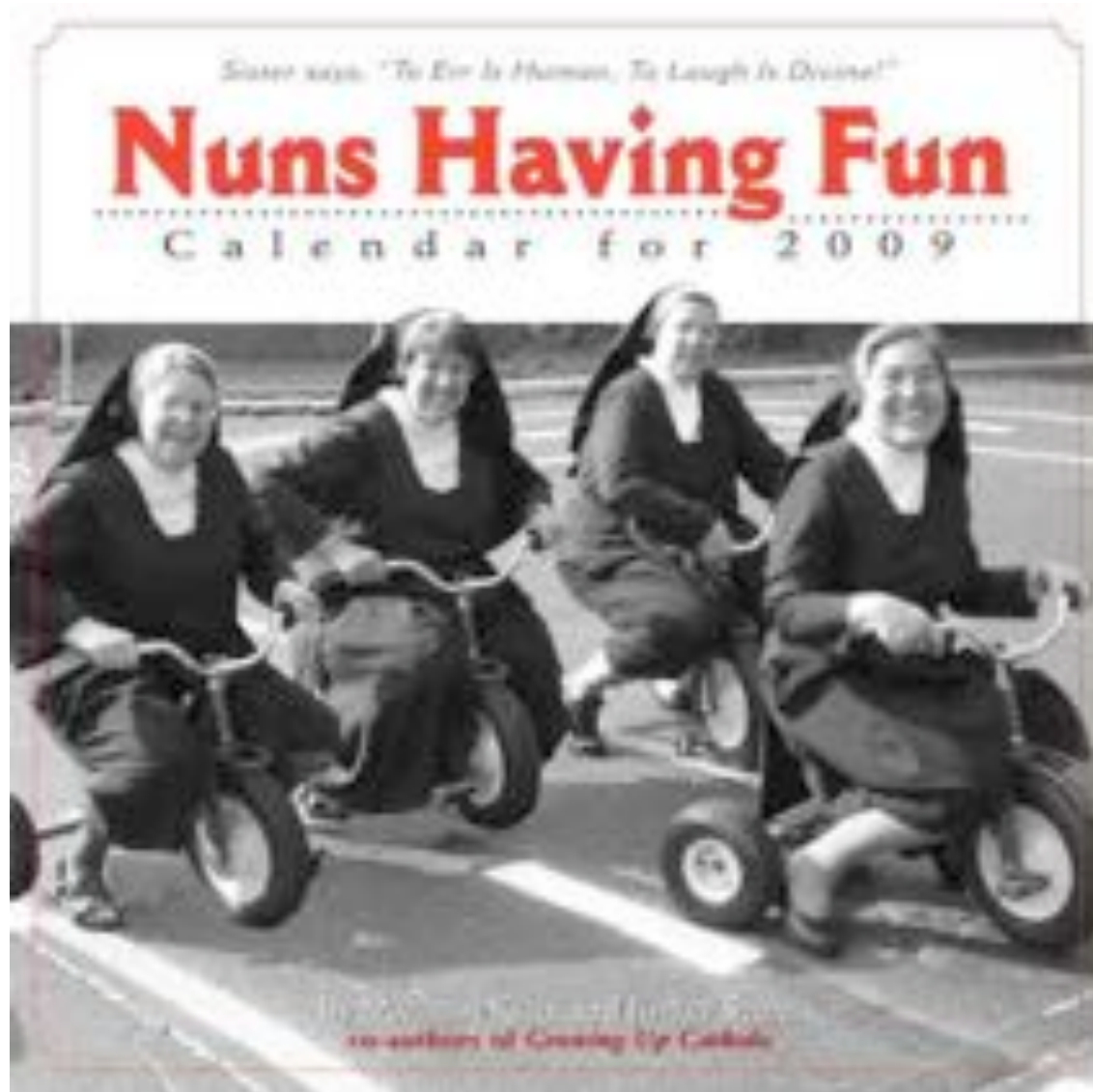
CSE 545, Spring 2019

# Whatever your impression of the 331





Hopefully it was fun!



# Thanks!



Except of course, HW 10, presentations and the final exam