#### Lecture 11

CSE 331 Sep 21, 2018

# Mini Project group due Monday!



## HW 3 is out!

#### Homework 3

Due by 11:59pm, Thursday, September 27, 2018.

Make sure you follow all the homework policies.

All submissions should be done via Autolab.

The support page for matrix vector multiplication should be very useful for this homework.

#### Sample Problem

#### The Problem

For this and the remaining problems, we will be working with # x # matrices (or two-dimensional arrays). So for example the following is a 3 x 3 matrix

$$\mathbf{M} = \begin{pmatrix} 1 & 2 & -3 \\ 2 & 9 & 0 \\ 6 & -1 & -2 \end{pmatrix},$$

## Support page is very imp.

Support Pages +

#### **Matrix Vector Multiplication**

Autoiste

Martrix-vector multiplication is one of the most commonly used operations in real life. We unfortunately won't be able to talk about this in CSE 331 lectures, so this page is meant as a substitute. We will also use this as an excuse to point out how a very simple property of numbers can be useful in speeding up algorithms.

#### Background

In this note we will be working with matrices and vectors. Simply put, matrices are two dimensional arrays and vectors are one dimensional arrays (or the "usual" notion of arrays). We will be using notation that is consistent with array notation. So e.g. a matrix A with w rows and w columns (also denoted as an  $w \times w$  matrix) will in code be defined as int [][] A we new int[n] [n] (assuming the matrix stores integers). Also a vector x of size win code will be declared as int []  $x \times we wint[n]$  (again assuming the vector contains integers). To be consistent with the array notations, we will denote the entry in A corresponding to the *i*th row and *j*th column as A[x][y] (or A[[i][j]]). Similarly, the *i*th entry in the vector x will be denoted as x[y] (or x[[i]]). We will follow the array convention assume that the indices *i* and *j* start at 0.

If you want a refresher on matrices, you might want to start with this Khan academy video (though if you are comfortable with the array analogy above you should not really need much more for this note):

### Solutions to HW 2

#### Handed out at the end of the lecture

## Formally define everything



http://imgs.xkcd.com/comics/geeks\_and\_nerds.png

### Distance between u and v

Length of the shortest length path between u and v



Distance between RM and BO? 1

#### Tree

Connected undirected graph with no cycles



#### **Rooted Tree**



#### A rooted tree



Let the rest of the tree hang under "gravity"

### Rest of Today's agenda

Prove n vertex tree has n-1 edges

Algorithms for checking connectivity

## Checking by inspection



## What about large graphs?

![](_page_12_Figure_1.jpeg)

Are s and t connected?

## Brute-force algorithm?

![](_page_13_Figure_1.jpeg)

## Algorithm motivation

![](_page_14_Picture_1.jpeg)