Lecture 7

CSE 331 Sep 12, 2018

Things to remember

Make sure you follow the HW policies

If by chance you violated any, just don't submit

Make sure you clearly demarcate your submission

Use/follow the provided template

Check your PDF submits

Make sure to preview your PDF submission to Autolab!

A corrupted PDF or Word will get you a zero on that question

Your PDFs cannot be more than 3MB big

GS algo outputs a stable matching

Last lecture, GS outputs a perfect matching S

Lemma 3: S has no instability

Reading Assignment for today

note 🖈	stop following	123 views
Reading/watching assignment for Wednesday lecture		
So, another reading assignment for y'all. On Wednesday, I will go over the proof of Lemma 3 (i.e. the instability) a bit quickly on slides.	he output of GS algorith	mS has no
It would be useful if you could read up the proof from the book or you can watch the lecture video #pin lectures	from last year.	
edit good note 1	Updated 1 day a	go by Atri Rudra

Proof technique de jour Proof by contradiction



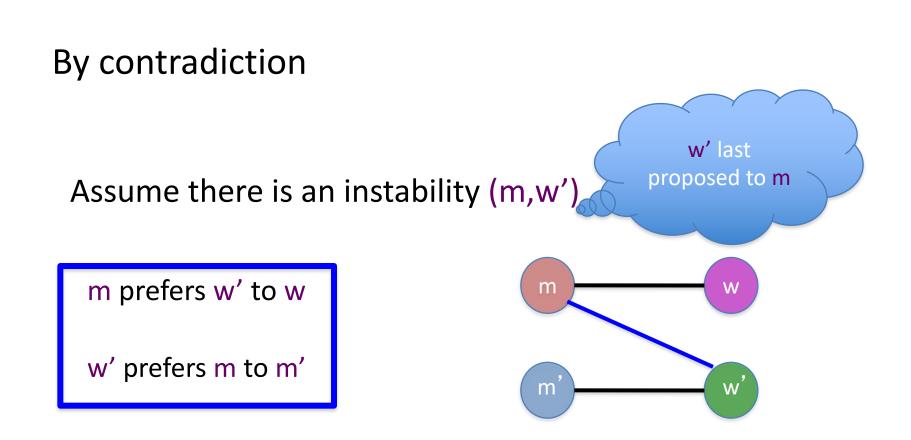
Source: 4simpsons.wordpress.com

Two obervations

Obs 1: Once m is engaged he keeps getting engaged to "better" women

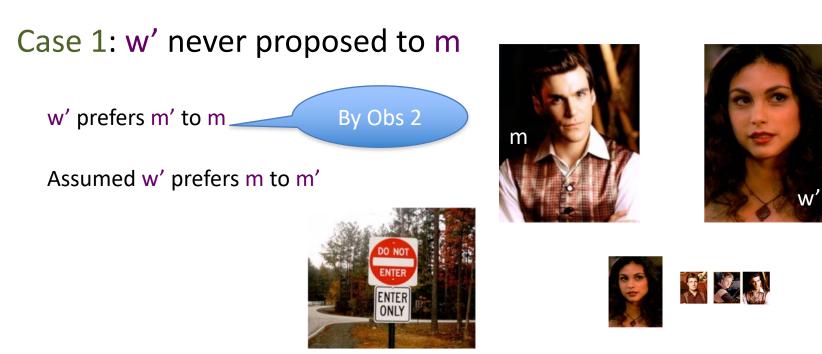
Obs 2: If w proposes to m' first and then to m (or never proposes to m) then she prefers m' to m

Proof of Lemma 3



Contradiction by Case Analysis

Depending on whether w' had proposed to m or not



Source: 4simpsons.wordpress.com

Case 2: w' had proposed to m

Case 2.1: m had accepted w' proposal

m is finally engaged to w

Thus, m prefers w to w'



4simpsons.wordpress.com







By Obs 1

By Obs 1

Case 2.2: m had rejected w' proposal

m was engaged to w'' (prefers w'' to w') By Obs 1

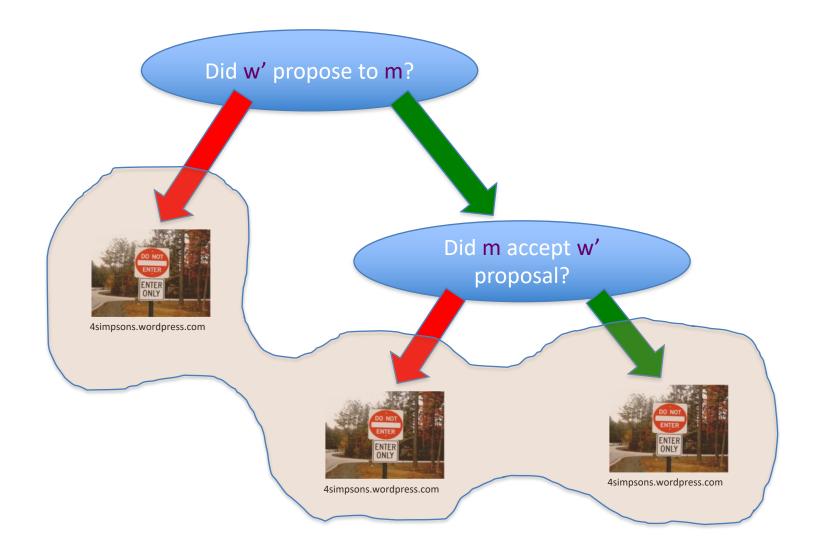
m is finally engaged to w (prefers w to w"____

m prefers w to w'

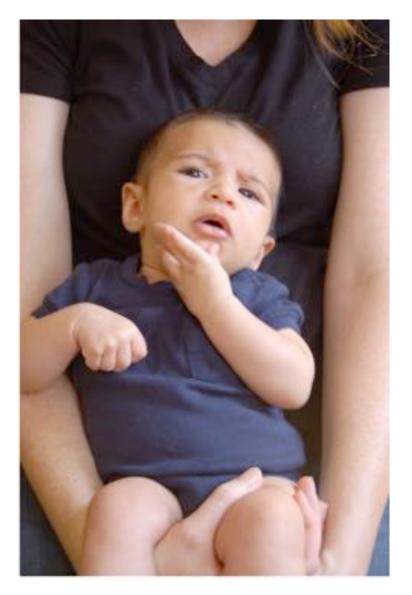


4simpsons.wordpress.com

Overall structure of case analysis



Questions?

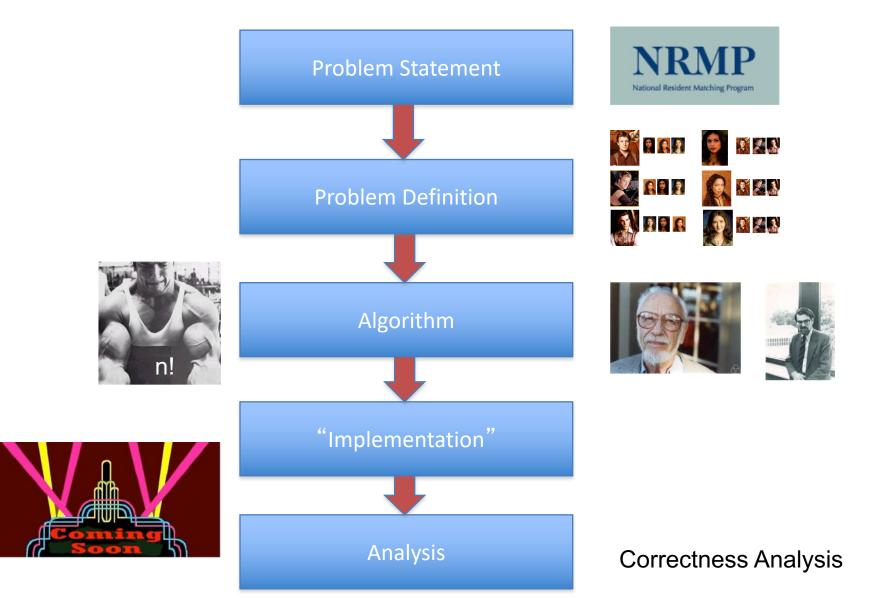


Extensions

Fairness of the GS algorithm

Different executions of the GS algorithm

Main Steps in Algorithm Design

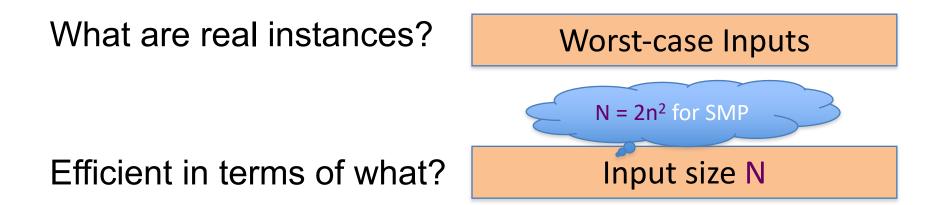


Definition of Efficiency

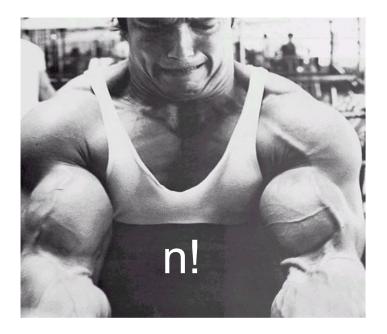
An algorithm is efficient if, when implemented, it runs quickly on real instances

Implemented where?





Definition-II



Analytically better than brute force

How much better? By a factor of 2?

Definition-III

Should scale with input size

If N increases by a constant factor, so should the measure



Polynomial running time

At most c·N^d steps (c>0, d>0 absolute constants)

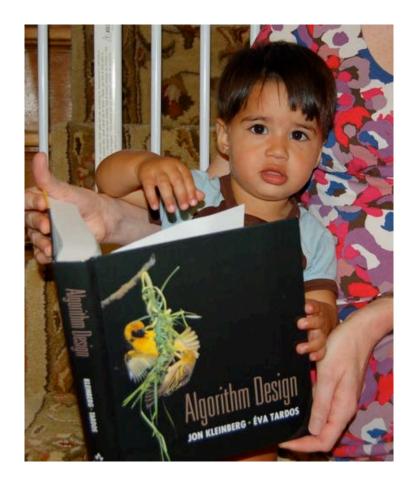
Step: "primitive computational step"

More on polynomial time

Problem centric tractability

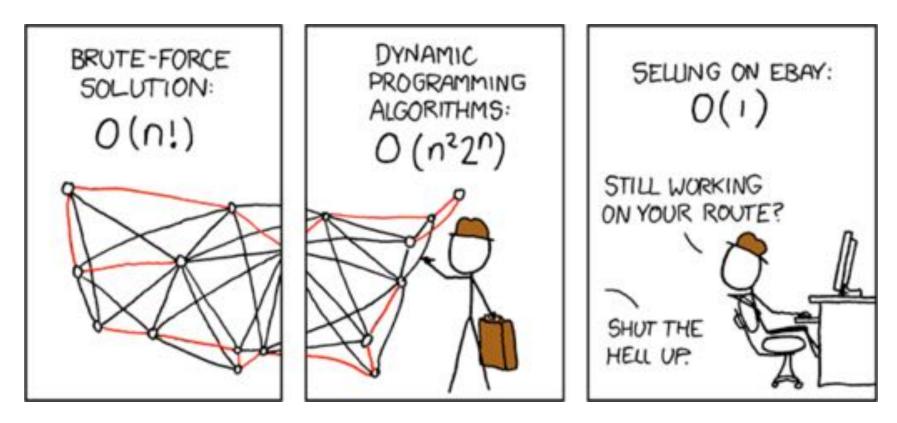
Can talk about problems that are not efficient!

Reading Assignments



Sections 1.2, 2.1, 2.2 and 2.4 in [KT]

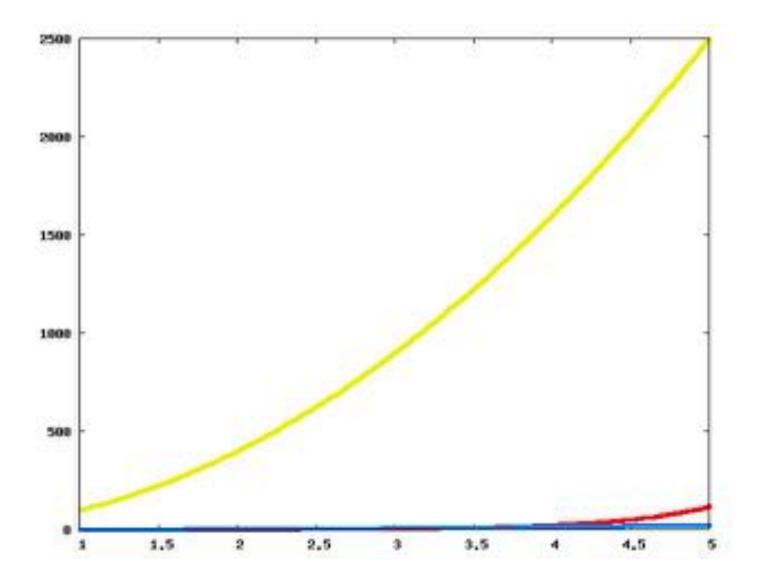
Asymptotic Analysis

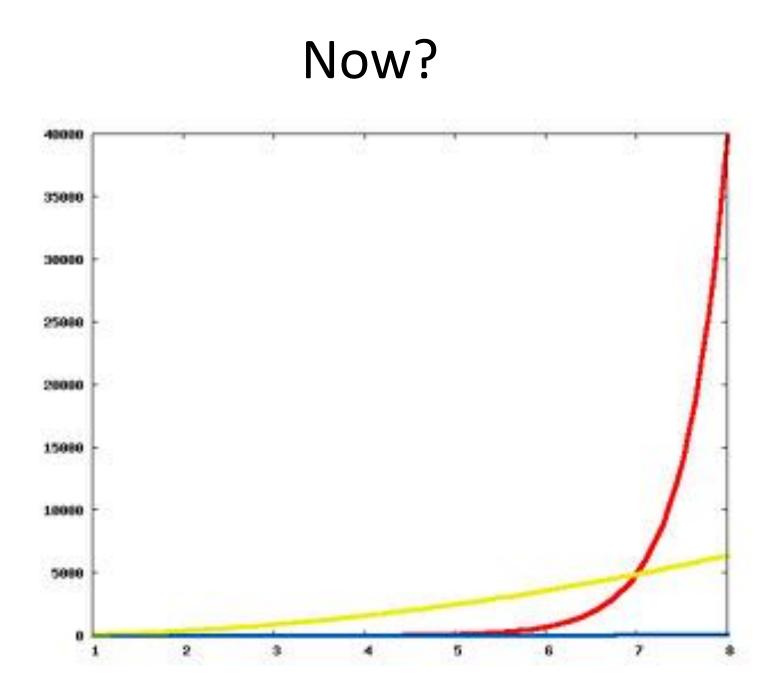


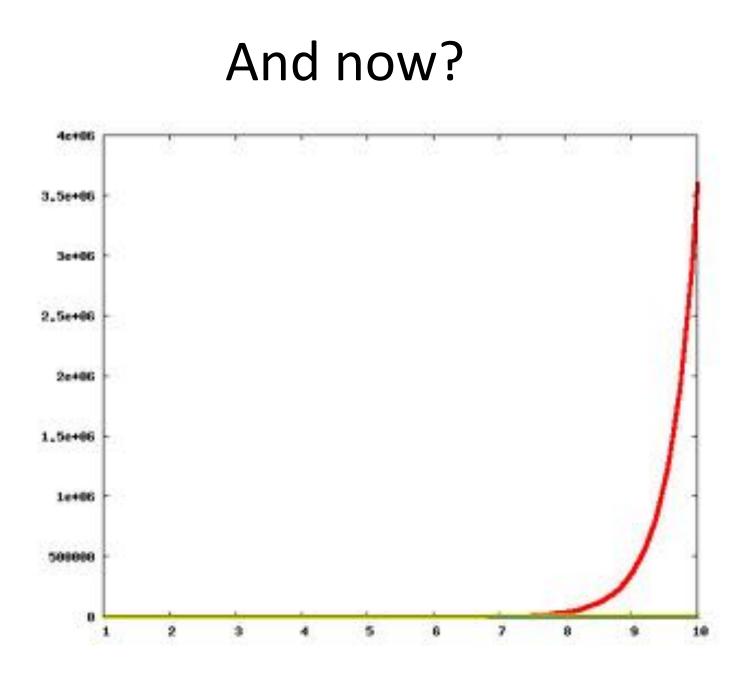
Travelling Salesman Problem

(http://xkcd.com/399/)

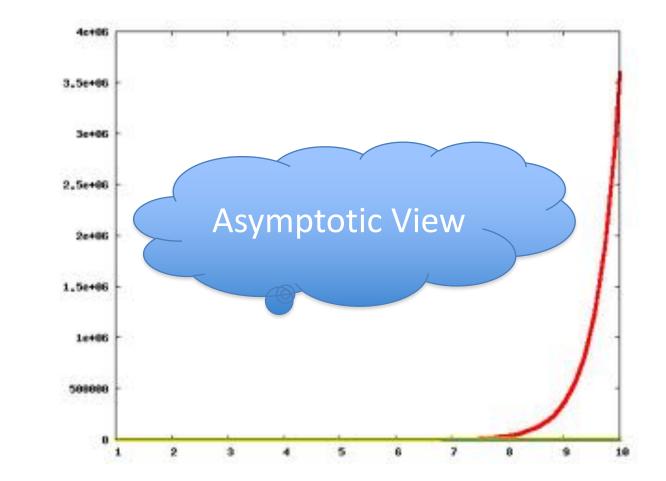
Which one is better?

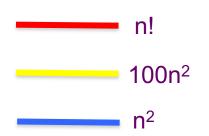






The actual run times





Asymptotic Notation

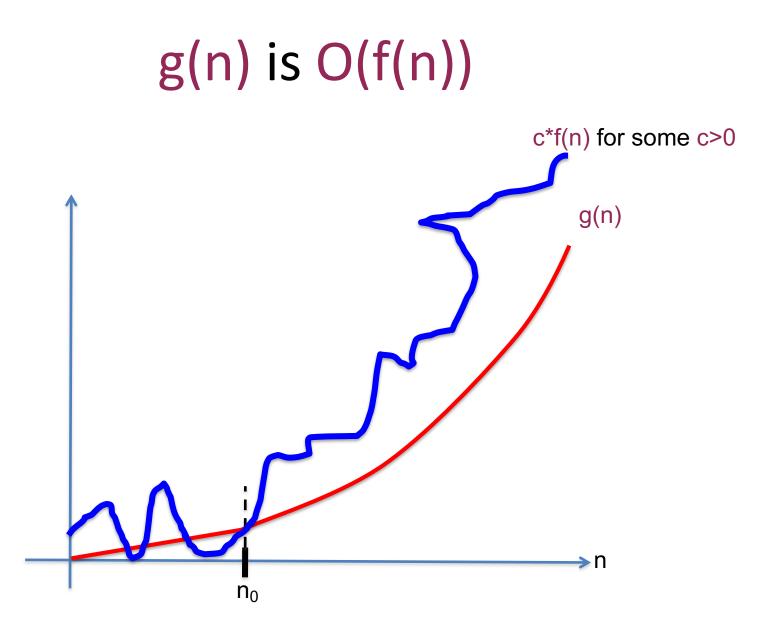


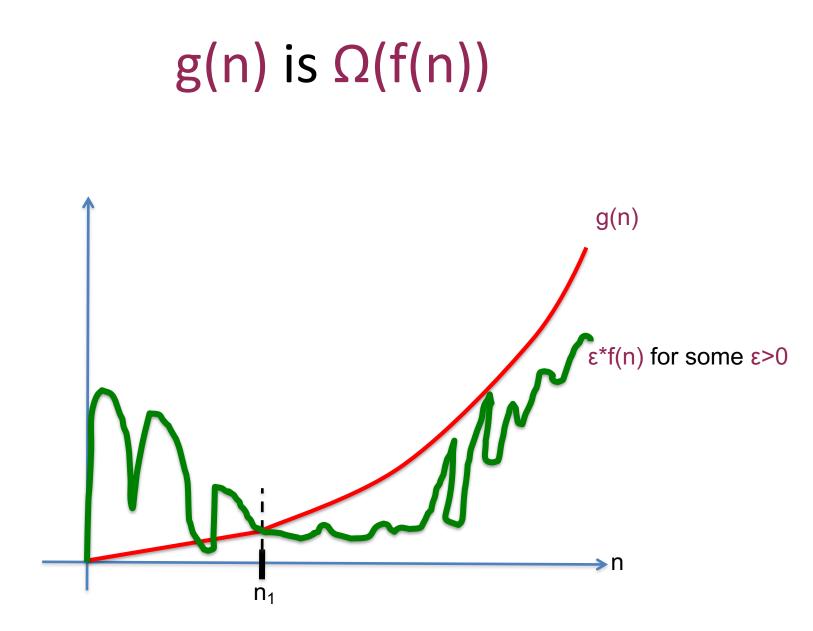
 \leq is O with glasses \geq is Ω with glasses = is Θ with glasses

Another view

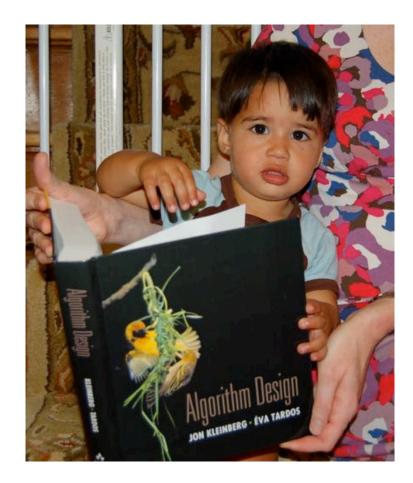
remain anonymous on the web, let me know). Silly way to remember Asymptotic notation... Stick figure: Dig 0 "Ceiling of functn" Big 0 Big 0 Blw Big-04 Big.D Dig 12 Floor of functn" feet remain anonymous on the web, let me know).

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Reading Assignments



Sections 1.1, 1.2, 2.1, 2.2 and 2.4 in [KT]