## Lecture 25

CSE 331
Oct 28, 2019

## Mid-term temp grade

Out by tomorrow night

## HW 5 grading

Hopefully by tonight

## Lecture on Friday

## Ashish Tyagi from Goldman Sachs this Friday lecture

A gentle reminder from @960 about Ashish Tyagi speaking for the first 10 mins of the lecture on Friday. Ashish was a TA for 331 in Fall 16 and now works at Goldman Sachs. Ashish's presentation/chat will not be recorded so you'll have to come to class if you want to listen to him :-)

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logistics lectures
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## Course next semester

## Algorithms are here. What's next?

Next semester I am teaching a CSE 410 special topics with title above. A description is at the end of the post. Let me know if you have any Qs on this [and before you ask, no, this is not a proof based course :-)] My replies might be a bit delayed for the rest of the week but in worst-case l'll reply back next week.

If you are interested, you should register for Section A1. Also see Shelly's email for details on how to force register etc.

CSE 410: Title: Algorithms Have Arrived - What's next? (Section A1)
Topic: Algorithms make decisions in all parts of our lives, starting from the mundane (e.g. Netflix recommending us movies/TV shows), to the somewhat more relevant (e.g. algorithms deciding which ads Google shows you) to the downright worrisome (e.g. algorithms deciding the risk of a person who is arrested committing a crime in the future). Whether we like it or not, algorithms are here to stay due to the economic benefit of automation provided by algorithms.
Professor Atri Rudra

## Prerequisites

Section A1 (which is for CSE majors) has a pre-requisite of CSE 331 OR CSE 474. Sect junior in their major). For both sections, willingness to think beyond your usual boxe

Description: While the benefits of using algorithm to make automated decision

This class will look into various algorithms in use in real life and go into deptl the hope is that this course will open their eyes to societal implications of techry algorithms/math cannot be biased" is at best a cop-out). For students who ar a better understanding of the technical/mathematical underpinnings of these you cannot accurately judge the societal impacts of an algorithm).
Overall the hope is that students who will build the technology of the future will be equip

> Potentially research
> project on use of AI in foster care system
e-requisites (besides being a een harmful effects.
technologically inclined, see why claiming "But
that this class will give them level, how these algorithms work folks building technology need to be activists but when presented with two viable technical option the future decision-makers can make more informed decisions on how algorithms can impact othe themselves but they should be able to understand how algorithms interacts with real life data). CSE majors should register in Section A1.
\#pin

## Divide and Conquer

Divide up the problem into at least two sub-problems

Recursively solve the sub-problems
"Patch up" the solutions to the sub-problems for the final solution

## Improvements on a smaller scale

Greedy algorithms: exponential $\rightarrow$ poly time
(Typical) Divide and Conquer: $\mathrm{O}\left(\mathrm{n}^{2}\right) \rightarrow$ asymptotically smaller running time

## Multiplying two numbers

Given two numbers $a$ and $b$ in binary

$$
a=\left(a_{n-1}, . ., a_{0}\right) \text { and } b=\left(b_{n-1}, \ldots, b_{0}\right)
$$

Compute $\mathrm{c}=\mathrm{ax} \mathrm{b}$

## Elementary <br> school <br> algorithm is <br> $O\left(n^{2}\right)$

## The current algorithm scheme



$$
\begin{aligned}
& T(n) \leq 4 T(n / 2)+c n \\
& T(1) \leq c
\end{aligned}
$$

## The key identity

$$
a^{1} b^{0}+a^{0} b^{1}=\left(a^{1}+a^{0}\right)\left(b^{1}+b^{0}\right)-a^{1} b^{1}-a^{0} b^{0}
$$

## The final algorithm

Input: $\mathrm{a}=\left(\mathrm{a}_{\mathrm{n}-1}, \ldots, \mathrm{a}_{0}\right)$ and $\mathrm{b}=\left(\mathrm{b}_{\mathrm{n}-1}, \ldots, \mathrm{~b}_{0}\right)$
Mult (a, b)

$$
\begin{aligned}
& \text { If } n=1 \text { return } a_{0} b_{0} \\
& a^{1}=a_{n-1}, \ldots, a_{[n / 2]} \text { and } a^{0}=a_{[n / 2]-1}, \ldots, a_{0}
\end{aligned}
$$

Compute $b^{1}$ and $b^{0}$ from $b$
$x=a^{1}+a^{0}$ and $y=b^{1}+b^{0}$
Let $p=\operatorname{Mult}(x, y), D=\operatorname{Mult}\left(a^{1}, b^{1}\right), E=\operatorname{Mult}\left(a^{0}, b^{0}\right)$
$F=p-D-E$
return $D \cdot 2^{2[n / 2]}+F \cdot 2^{[n / 2]}+E$
$T(1) \leq c$
$\mathrm{T}(\mathrm{n}) \leq 3 \mathrm{~T}(\mathrm{n} / 2)+\mathrm{cn}$
$\mathrm{O}\left(\mathrm{n}^{\left.\left.\log _{2}{ }^{3}\right)=\mathrm{O}\left(\mathrm{n}^{1.59}\right), ~\right) ~(1)}\right.$
run time

All green operations are $O(n)$ time
$a \cdot b=a^{1} b^{1} \cdot 2^{2[n / 2]}+\left(\left(a^{1}+a^{0}\right)\left(b^{1}+b^{0}\right)-a^{1} b^{1}-a^{0} b^{0}\right) \cdot 2^{[n / 2]}+a^{0} b^{0}$

