# Lecture 27 

CSE 331
Nov 4, 2022

## Coding P2 due TODAY

| Fri, Nov 4 |  | [KT, Sec 5.4] (Project (Problem 2 Coding) iny |
| :---: | :---: | :---: |
| Mon, Now 7 | Weighted Interval Scheduling $\mathrm{P}^{2 / 1} \mathrm{P}^{\prime 71} \mathrm{C}^{17} \mathrm{x}^{2}$ | [KT, Sec 6.1] (Project (Problem 2 Derlection) in) |
| Tuen, Now 8 |  | (HW 6 out) |
| Wed, Now 9 | Recursive algorithm for weighted interval scheduling problem $\mathrm{B}^{21} \mathrm{C}^{17} \mathrm{c}^{17} \mathrm{x}^{4}$ | [KT, Sec 6.1] |
| Fri, Nov 11 | Subset sum problem $\mathrm{D}^{2 / 21} \mathrm{C}^{7 / 1} \mathrm{C}^{181} \mathrm{P}^{2 / 17} \mathrm{x}^{2}$ | [ KT , Sec 6.1, 6.2, 6.4] |
| Mon, Nov 14 |  | [ KT, Sec 6.4] |
| Tue, Nov 15 |  | (HW 7 out, HW 5 inf |
| Wod, Nov 16 | Shortest path problem $\mathrm{D}^{221} \mathrm{D}^{872} \mathrm{C}^{811} \mathrm{D}^{817} \mathrm{x}^{2}$ | [ KT, Sec 6.8] |
| Fri, Nov 18 |  | [KT, Sec 6.8] |
| Mon, Nor 21 | The $P$ ve. NP problem $\mathrm{P}^{2 / 1} \mathrm{P}^{211}$ | [KT, Sec 8.1] |
| Wed, Now 23 | No class | Fall Recess |
| Fri, Nov 25 | No class | Fall Recess |
| Mon, Nov 28 | More on reductions $\mathrm{P}^{P 21} \mathrm{D}^{813}$ | [KT, Sec 8.1] |
| Tue, Nov 29 |  | (RW B out, HW 7 in) |
| Wed, Noy 30 | The SAT problem $\mathrm{D}^{221} \mathrm{D}^{213}$ | [ KT , Sec 8.2] |
| Fr, Dec 2 | NP-Completeress $\mathrm{C}^{2 / 1} \mathrm{D}^{17}$ | [KT, Sec. 8.3, 8.4] (Project (Probiem 3 Coding) in) |
| Mon, Dec 5 | k-coloring problem $\mathbf{C}^{2 / 21} \mathrm{C}^{711}$ | (KT, Sec B.7] (Oulz 2) <br> (Project (Problem 3 Deflectisn) ing) |

## Group formation instructions

## Autolab group submission for CSE 331 Project

The lowdown on submitting your project (especially the coding and reflection) problems as a group on Autolab.

Follow instructions


The instruction below are for Coding Problem 1
You will have to repeat the instructions below for EACH coding AND reflection problem on project on Autolab (with the appropriate changes to the actual problemp)

## Form your group on Autolab

Groups on Autolab will NOT be automatically created
You will have to form a group on Autolab by yourself (as a groupl. Aead on for indituctions on how to go about this.

## Make sure you are in your group

## Coding P1 due today

A perite meninder that fie fint voding probion is due by Ilisllon tonight


## 

 never lo be included.
## 

Tlat poed nolte

## Coding problem grading

## Please make sure you read the coding grading rubric correctly

Looks the few of your are not interperting how the grading for problems 2.5 morks (esa3).

Phease note that it your sevenue exactly matches the revenue of the optirnal solution for problem 1 you should be getting level 0 . Note that the ratio that determirnes your level is
(your solution's revenue - revenue of optimal Solution for Problem 1)
(four revenue - avevenue from optimal Solution for Problem 1)

If you revennue matches that of optimal sclution for problem 1 , your case the furnerator is 0 and hence your level will be 0.

## project

## OH today shortened to 30 mins



So sorry to do this but my Friday OH for Nov 4 will be for 30 mins from $12: 45-1: 15 \mathrm{pm}$. This change is only for this week and the Wed Ofts times will not change.

## office_hours

## Have fun @ UB Hacking!

## UB Hatking 2022

## Questions/Comments?



## Closest pairs of points

Input: $n 2-D$ points $P=\left\{p_{1}, \ldots, p_{n}\right\} ; p_{i}=\left(x_{i}, y_{i}\right)$

$$
\mathrm{d}\left(\mathrm{p}_{\mathrm{i}}, \mathrm{p}_{\mathrm{j}}\right)=\left(\left(\mathrm{x}_{\mathrm{i}}-\mathrm{x}_{\mathrm{j}}\right)^{2}+\left(\mathrm{y}_{\mathrm{i}}-\mathrm{y}_{\mathrm{j}}\right)^{2}\right)^{1 / 2}
$$

Output: Points p and q that are closest


## Dividing up P



First $\mathrm{n} / 2$ points according to the x -coord

## Recursively find closest pairs



# An aside: maintain sorted lists 

$P_{x}$ and $P_{y}$ are $P$ sorted by $x$-coord and $y$-coord
$Q_{x}, Q_{y}, R_{x}, R_{y}$ can be computed from $P_{x}$ and $P_{y}$ in $O(n)$ time

## An easy case



## Life is not so easy though



## Questions/Comments?



## Euclid to the rescue (?)

$$
d\left(p_{i}, p_{j}\right)=\left(\left(x_{i}-x_{j}\right)^{2}+\left(y_{i}-y_{j}\right)^{2}\right)^{1 / 2}
$$

The distance is larger than the $\mathbf{x}$ or $\mathbf{y}$-coord difference

## Life is not so easy though


$\delta=\min$ (blue, green)

## All we have to do now


$\delta=\min$ (blue, green)

## The algorithm so far...

Input: $n$ 2-D points $P=\left\{p_{1}, \ldots, p_{n}\right\} ; p_{i}=\left(x_{i}, y_{i}\right)$

$$
O(n \log n)+T(n)
$$

Sort $P$ to get $P_{x}$ and $P_{y}$
Closest-Pair ( $P_{x}, P_{y}$ )
On $\log \mathrm{n})$

$$
T(<4)=c
$$

If $\mathrm{n}<4$ then find closest point by brute-force

$$
T(n)=2 T(n / 2)+c n
$$ $Q$ is first half of $P_{x}$ and $R$ is the rest


$\mathrm{O}(\mathrm{n})$
Compute $\mathrm{Q}_{x}, \mathrm{Q}_{y}, \mathrm{R}_{x}$ and $\mathrm{R}_{y}$
On)
$O(n \log n)$ overall
$\left(q_{0}, q_{1}\right)=$ Closest-Pair $\left(Q_{x}, Q_{y}\right)$
$\left(r_{0}, r_{1}\right)=$ Closest-Pair $\left(R_{x}, R_{y}\right)$
$\mathrm{O}(\mathrm{n})$
$\delta=\min \left(d\left(q_{0}, q_{1}\right), d\left(r_{0}, r_{1}\right)\right)$
$\mathrm{O}(\mathrm{n})$
return Closest-in-box $\left(S,\left(q_{0}, q_{1}\right),\left(r_{0}, r_{1}\right)\right)$

## Rest of today's agenda

Implement Closest-in-box in O(n) time

