Lecture 4

CSE 331

Sep 7, 2022

Please do keep on asking Qs!

The only bad question is the one that is not asked!

Not just technical Qs but also on how the class is run

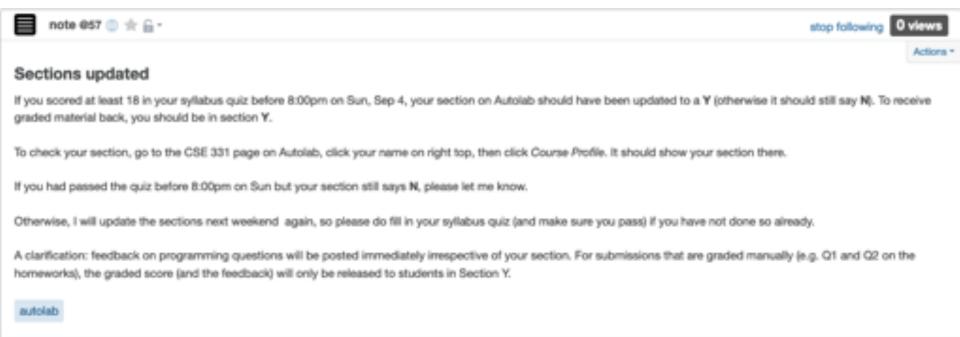
We're not mind readers



If you need it, ask for help



Syllabus Quiz (and sections)



Updated 10 seconds ago by Atri Rudra.

good note 0

Separate Proof idea/proof details

O Note

Notice how the solution below is divided into proof idea and proof details part. THIS IS IMPORTANT: IF YOU DO NOT PRESENT A PROOF IDEA, YOU WILL NOT GET ANY CREDIT EVEN IF YOUR PROOF DETAILS ARE CORRECT.

Proof Idea

As the hint suggests there are two ways of solving this problem, (i'm presenting both the solutions but of course you only need to present one.)

We begin with the approach of reducing the given problem to a problem you have seen earlier.

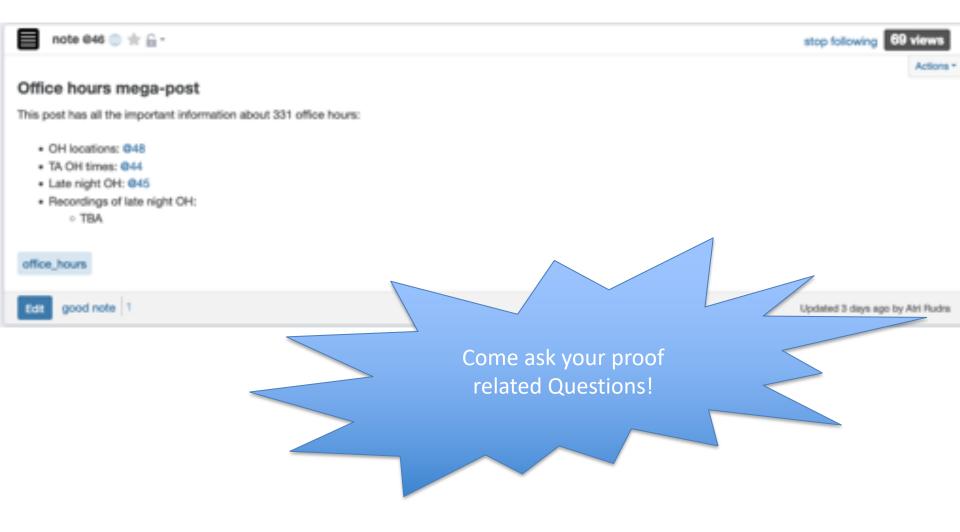
Build the following complete binary tree: every internal node in the tree represents a "parent" RapidGrower while its two children are the two RapidGrowers it divides itself into. After a seconds this tree will have height a and the number of RapidGrowers in the container after a seconds is the number of leaf nodes these complete binary tree has, which we know is 2°. Hence, the claim is correct.

The proof by induction might be somewhat simpler for this problem if you are not comfortable with reduction. In this case let R(s) be the number of RapidGrowers after s seconds. Then we use induction to prove that $R(s) = 2^s$ while using the fact that $2 \cdot 2^s = 2^{s+1}$.

Proof Details

We first present the reduction based proof. Consider the complete binary tree with height s and call it T(s). Further, note that one can construct T(s+1) from T(s) by attaching two children nodes to all the leaves in T(s). Notice that the newly added children are the leaves of T(s+1). Now assign the root of T(0) as the original RapidGrower in the container. Further, for any internal node in T(s) ($s \ge 0$), assign its two children to the two RapidGrowers it divides itself into. Then note that there is a one to one correspondence between the RapidGrowers after s seconds and the leaves of T(s). Then we use the well-known fact (cite your 191/250 book here with the exact place where one can find this fact): T(s) has 2' leaves, which means that the number of RapidGrowers in the container after s seconds is 2', which means that the claim is correct.

Office hours finalized



Late night office hour starts tonight!

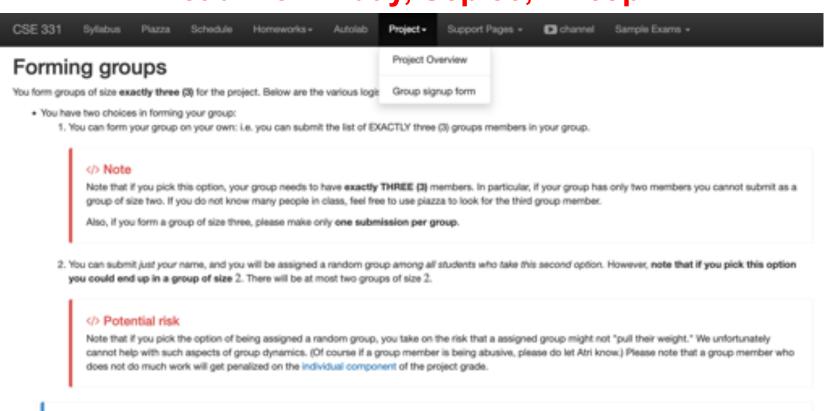


1st True/False poll



Register your project groups

Deadline: Friday, Sep 30, 11:59pm



You need to fill in the form for group composition by 11:59pm on Friday, September 30.

Submitting your group composition

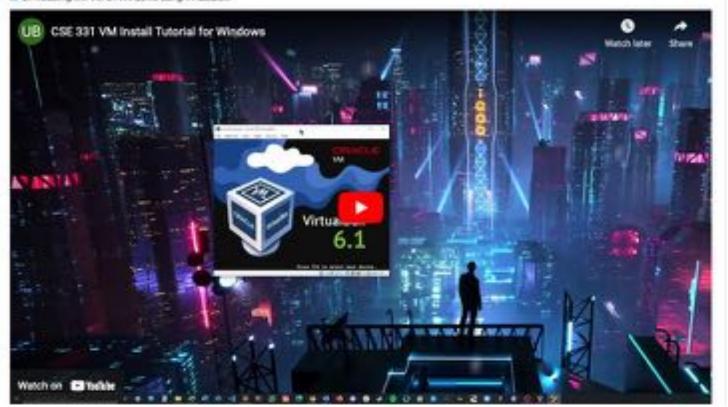
the same the same to be form for group composition by the deadline, then you get a zero for the entire project.

Use this Google form I to submit your group composition (the form will allow you to pick one of the two options above).

Update on VM

Using VM Image on Windows

If plan to not the VM on Windows then Fall 2022 onwards, we recommend that you rub it using birtual Box (and eat VMMare). Here is a wall-frough video by Nick Minor (7 on installing the VM on Windows using VMusiBox.



Using VM Image on MacOS

Unfortunately, it looks like Virtualities does not work that well on MacOS. We're tooking into foxes.

In the meantime, using VMMisre on MacCS might be the ibly option. If you already have a VMMisre license that lasts until the semester lasts, then you should be all set. If you need a license please email Abri ASAP.

Piazza Response policy

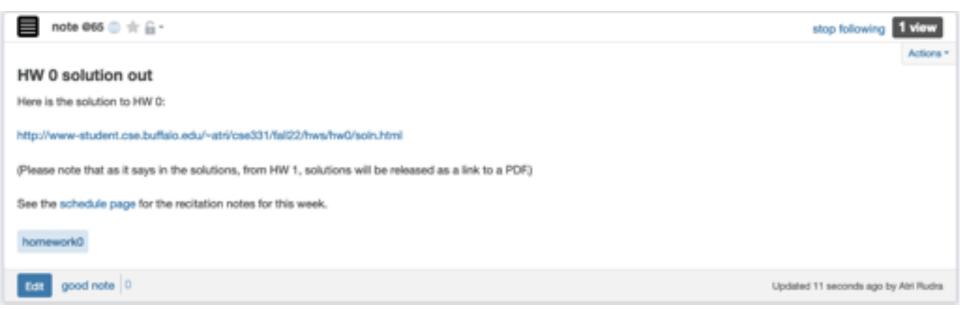
Piazza Response policy

Please note the following rules regarding response time to student questions on piazza:

- Any question posted between Friday at 5pm and Monday 9am might not get an answer from CSE 331 staff before Monday 9am.
- On weekdays, we will aim to respond to student question within four hours unless the question is posted between 7pm and 9am, in which case we might only be able to respond after 9am.

Please note that the above does not means that we will never answer questions posted in the evening/night times as mentioned above— it's just that we might not always be able to respond within four hours. Based on previous years, I do expect there to be reasonable response time in the evening times as well— it's just that OUR response times might be more variable.

Solutions to HW 0 out



Questions/Comments?



Incorrect Proof Details: Q1(b) on

Argument does not use ANYTHING about the problem statement!

HW0

Follows from part (a)

f perfect matchings with n men and n wo.



This assumes number of perfect matchings only depends on n

Inductive hypothesis: Assume that P(n-1) = (n-1)!

Inductive step: Note that P(n) = n*P(n-1) = n*(n-1)! = n!

What are the issues with the above "proof"?

Incorrect Proof Details: Q1(b) on HW0

Needs justification

Claim 1: Number of perfect matchings is = number of permutations of 1...n

Claim 2: Number of permutations of 1...n is n!

Claims 1 + 2 prove the result

Needs justification

Follow from 191 (?)

What are the issues with the above proof?

Proof by contradiction for Q1(a)

Assume for contradiction there is an example where number of perfect matchings depends on the identities of the meand women.

Let n =1 and consider two cases

(1)
$$M = \{BP\} \text{ and } W = \{JA\}$$

(2)
$$M = \{BBT\}$$
 and $W = \{AJ\}$

You can only assume things about the example directly implied by it being a counter-example

In both cases the number of perfect matchings is 1 = 1!

Hence contradiction.

There is NO contradiction

What are the issues with the above proof?

Questions/Comments?



Questions to think about

1) How do we specify preferences?

Preference lists

2) Ratio of applicant vs employers

1:1

3) Formally what is an assignment?

(perfect) matching

4) Can an employer get assigned > 1 applicant?

NO

5) Can an applicant have > 1 job?



6) How many employer/applicants in an applicants/employers preferences?

All of them

7) Can an employer have 0 assigned applicants?

NO

8) Can an applicant have 0 jobs?

NO

On matchings

Mal







Inara

Wash

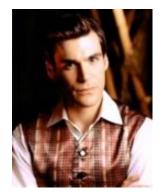






Zoe

Simon





Kaylee

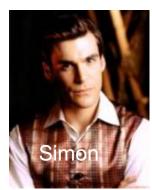
A valid matching













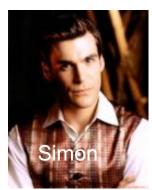
Not a matching













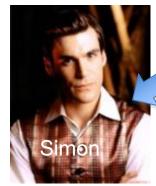
Perfect Matching













Questions/Comments?



Preferences























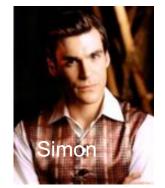


















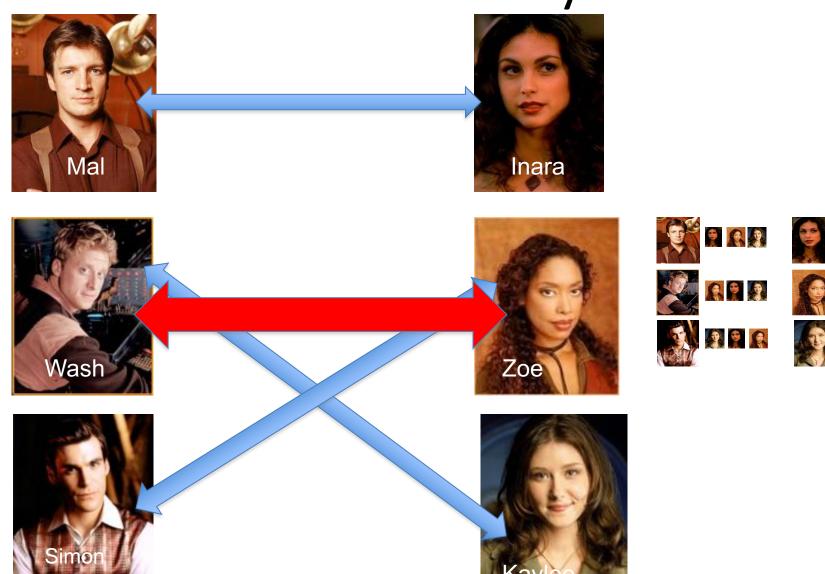








Instability



Back to the board...

