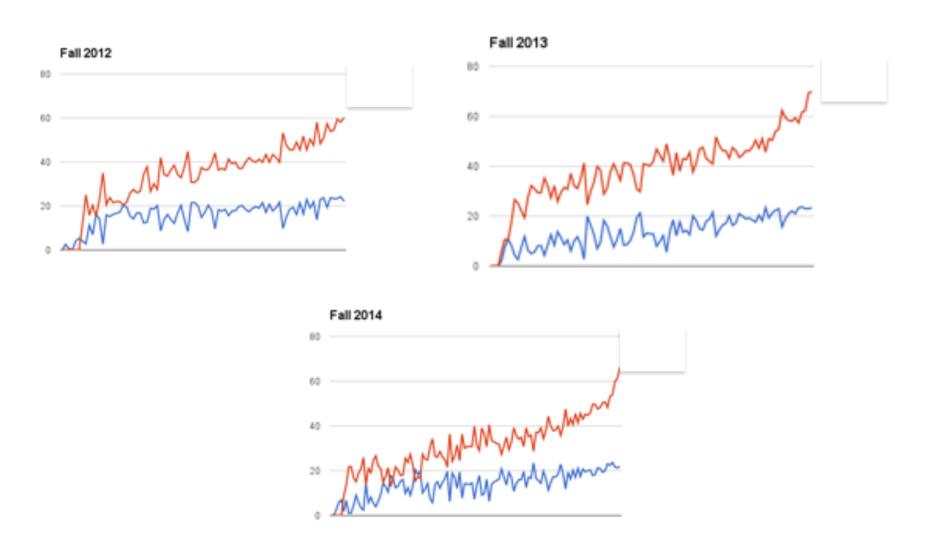
Lecture 5

CSE 331

Sep 9, 2022

Can you guess the correlation?



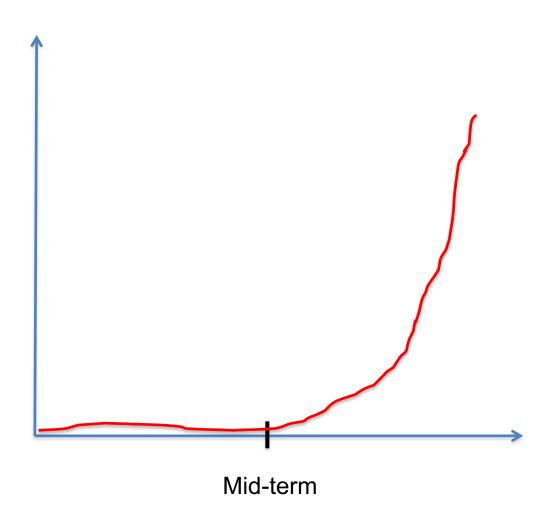
Another comment

Discomfort with proofs

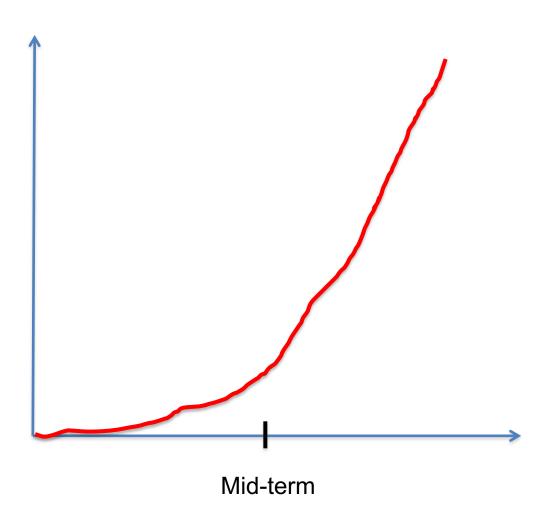
I will not cover proof basics in class anymore

Please read support pages and some utilize (next few) Office hours!

Lecture pace (until Fall 18)

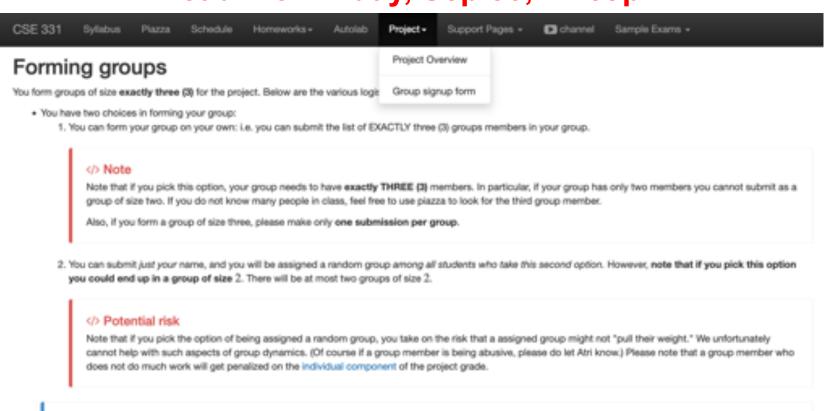


Lecture pace



Register your project groups

Deadline: Friday, Sep 30, 11:59pm



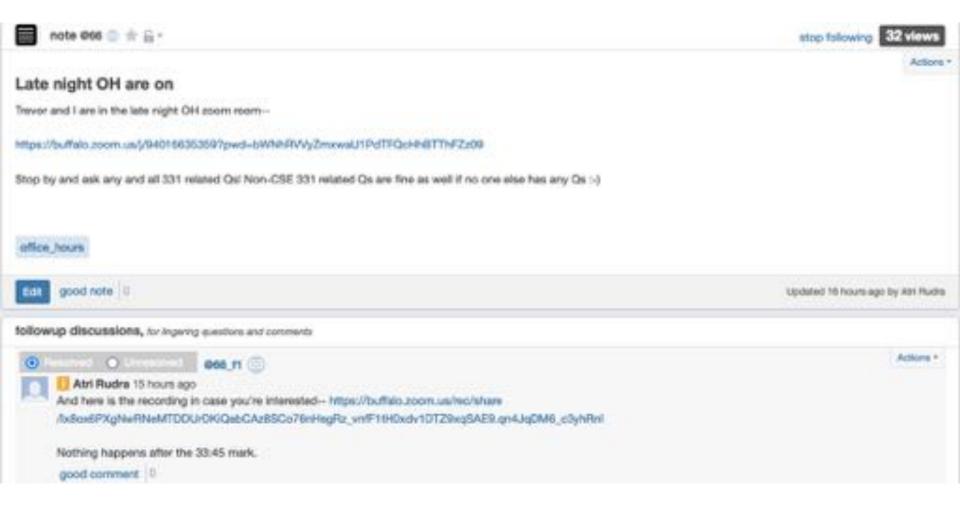
You need to fill in the form for group composition by 11:59pm on Friday, September 30.

Submitting your group composition

the same the same to be form for group composition by the deadline, then you get a zero for the entire project.

Use this Google form I to submit your group composition (the form will allow you to pick one of the two options above).

Do come to late night OH!



Questions/Comments?



(Perfect) Matching

A matching $S \subseteq M \times W$ such that following conditions hold:

S is a **set** of pairs (m,w) where m in M and w in W

exactly

- (1) For every woman w in W, exist at most one m such that (m,w) in S exactly
- (2) For every man m in M, exist at most one w such that (m,w) in S

Perfect matching

On matchings

Mal







Inara

Wash

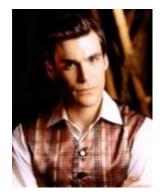






Zoe

Simon



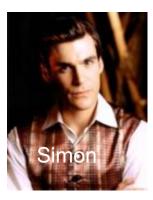


Kaylee

A valid matching













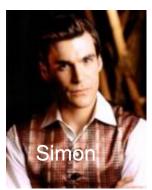
Not a matching













Perfect Matching













Preferences























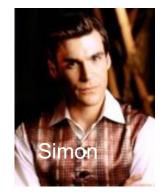


















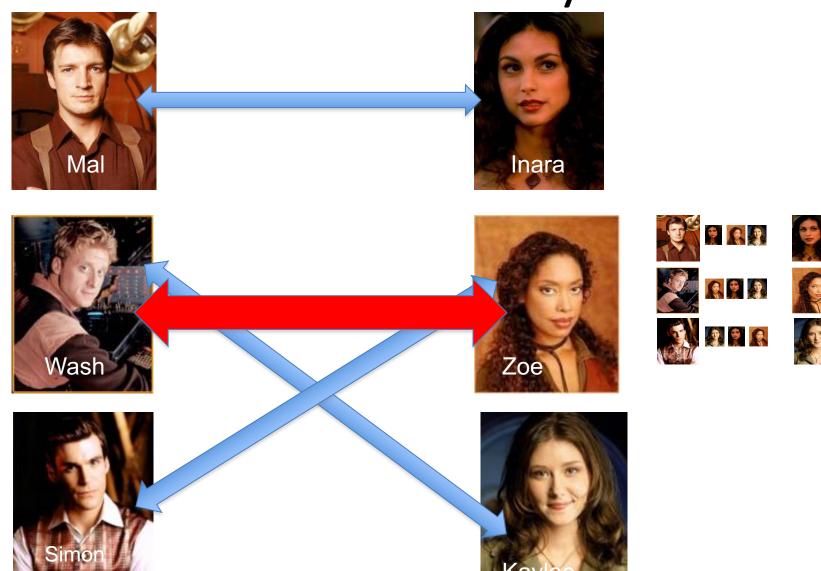








Instability



A stable matching

Even though BBT and JA are not very happy









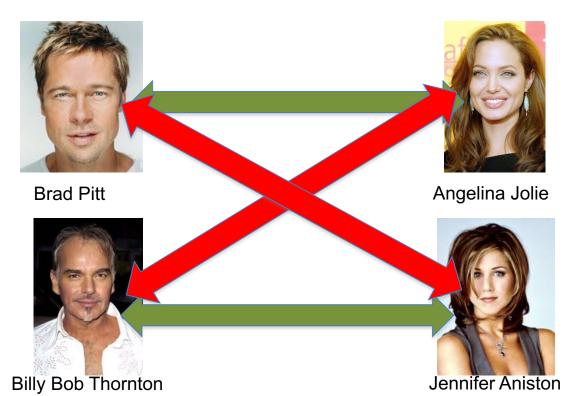












Two stable matchings



























Brad Pitt



Billy Bob Thornton



Angelina Jolie



Jennifer Aniston

Stable Matching problem

Set of men M and women W

Preferences (ranking of potential spouses)

Matching (no polyandry/gamy in M X W)

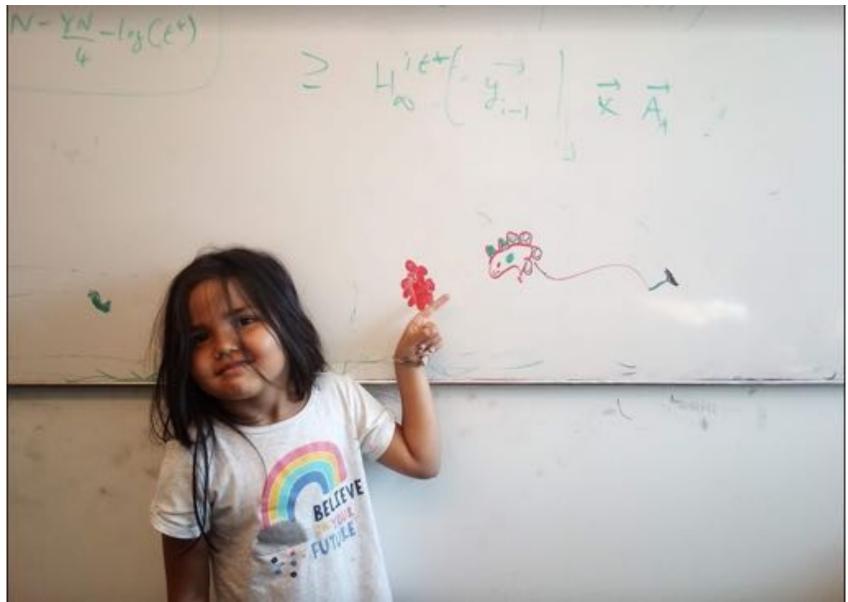
Perfect Matching (everyone gets married)

Instablity

Input: M and W with preferences **Output:** Stable Matching

Stable matching = perfect matching+ no instablity

Questions/Comments?



Two Questions

Does a stable marriage always exist?

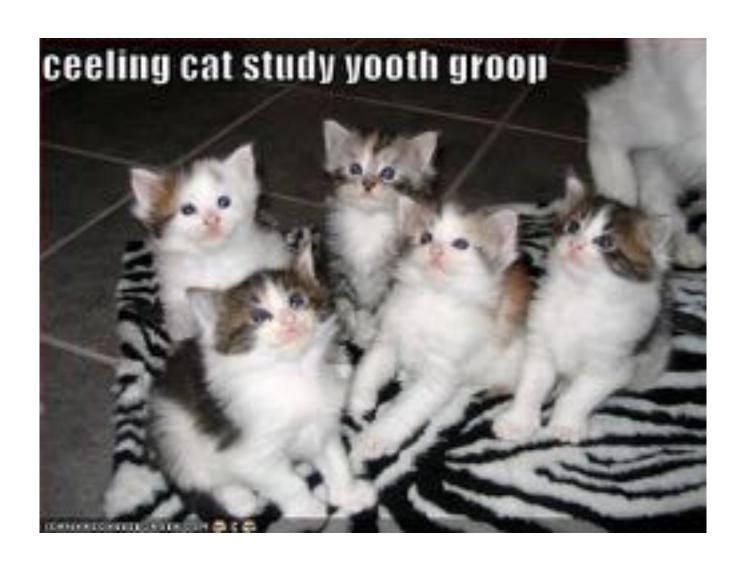
If one exists, how quickly can we compute one?

Today's lecture

Naïve algorithm

Gale-Shapley algorithm for Stable Marriage problem

Discuss: Naïve algorithm!



The naïve algorithm

Incremental algorithm to produce all n! prefect matchings?

Go through all possible perfect matchings S

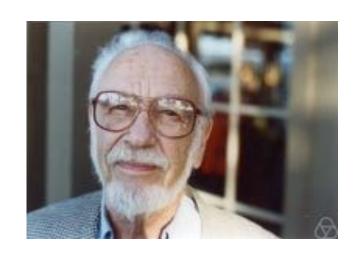
If S is a stable matching

then Stop



Else move to the next perfect matching

Gale-Shapley Algorithm



David Gale



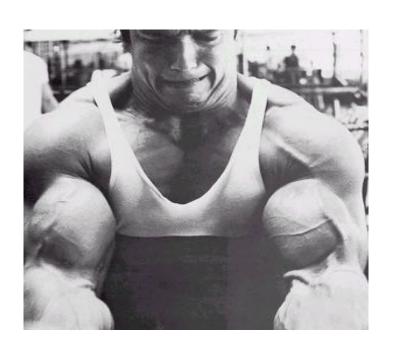
Lloyd Shapley

O(n²) algorithm

Moral of the story...







Questions/Comments?



Rest of today's agenda

Gale Shapley (GS) algorithm

Run of GS algorithm on an instance